

# Multimedia Forensics for Traitors Tracing



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# Talk Overview

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- **Digital Fingerprinting and Traitors Tracing**
  - Motivation of digital fingerprinting
  - Background: e.g. additive spread spectrum embedding
  - Collusion attacks: collusion schemes, analysis and comparison
- **Orthogonal Fingerprinting and variations**
  - Capacity of tracing colluders by using orthogonal modulation
  - Group-oriented fingerprinting
- **Coded Fingerprinting**
  - Anti-collusion codes and code modulated fingerprints
  - Colluder identification schemes
- **Traitors Behavior Dynamics in Collusion**



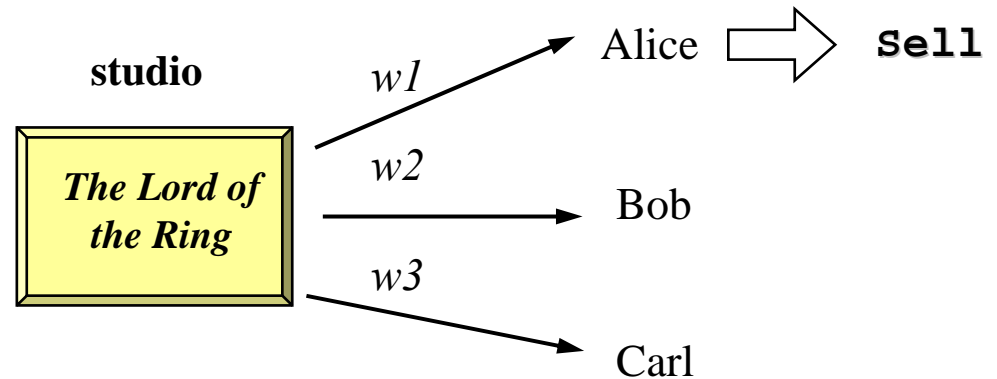
# ***Digital Fingerprinting and Traitors Tracing***



# Digital Fingerprinting and Tracing Traitors

- Leak of information as well as alteration and repackaging poses serious threats to government operations and commercial markets

- e.g., pirated content or classified document

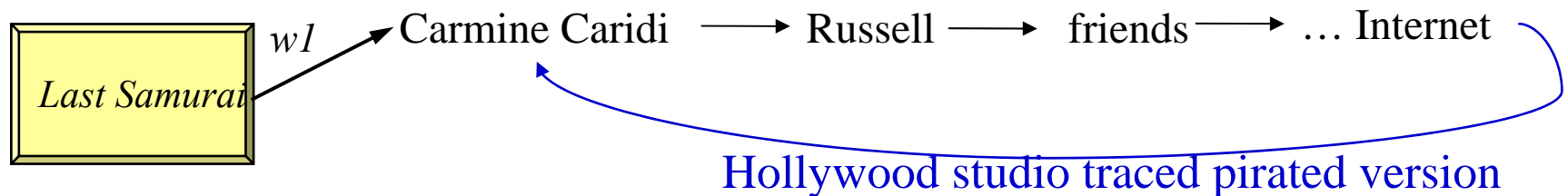


- Promising countermeasure: robustly embed digital fingerprints

- Insert ID or “fingerprint” (often through conventional watermarking) to identify each user
- Purpose: deter information leakage; digital rights management(DRM)
- Challenge: imperceptibility, robustness, tracing capability

# Case Study: Tracing Movie Screening Copies

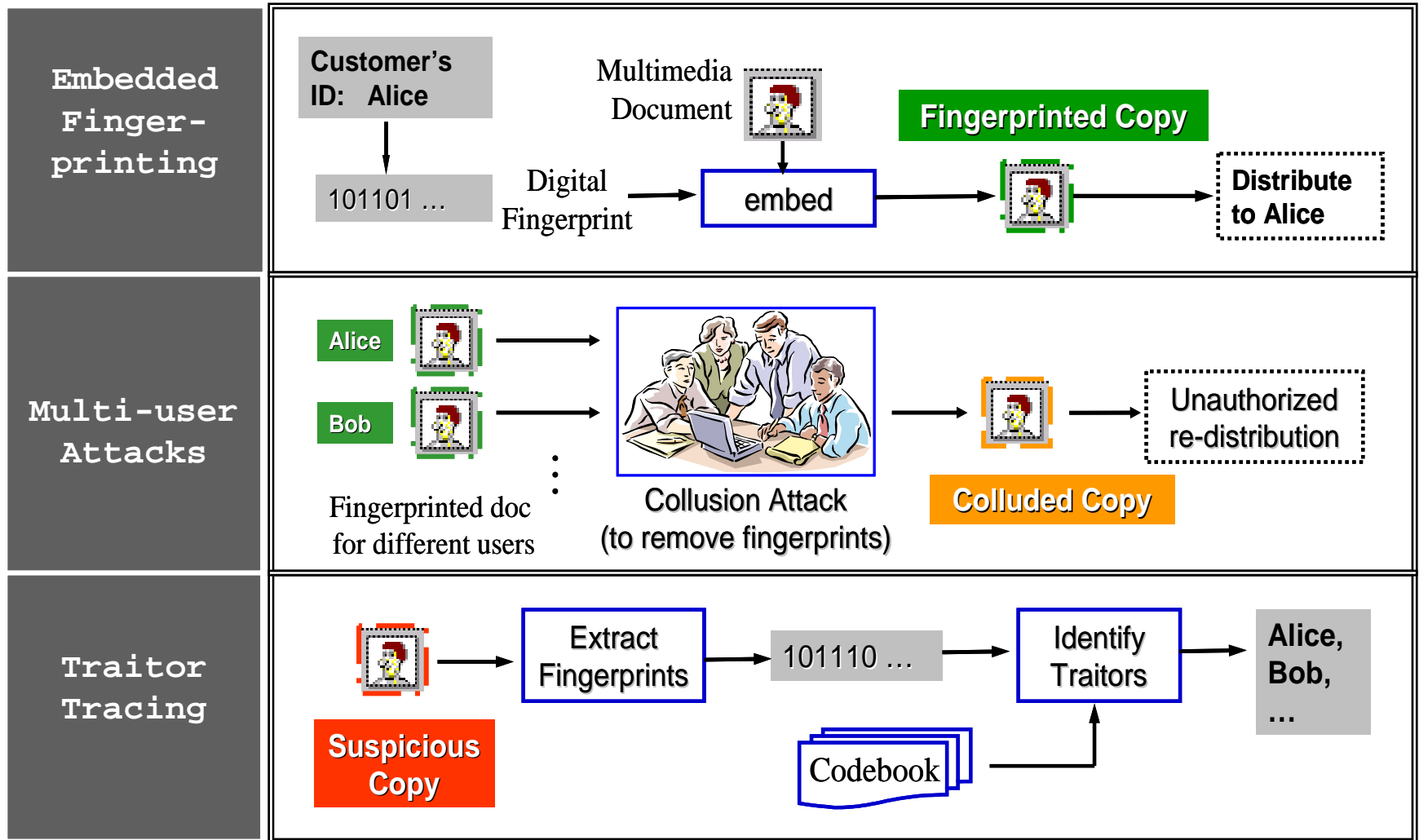
- Potential civilian use for digital rights management (DRM)
  - ◆ *Copyright industry – \$500+ Billion business ~ 5% U.S. GDP*
- Alleged Movie Pirate Arrested (23 January 2004)
  - A real case of a successful deployment of 'traitor-tracing' mechanism in the digital realm
  - Use invisible fingerprints to protect screener copies of pre-release movies



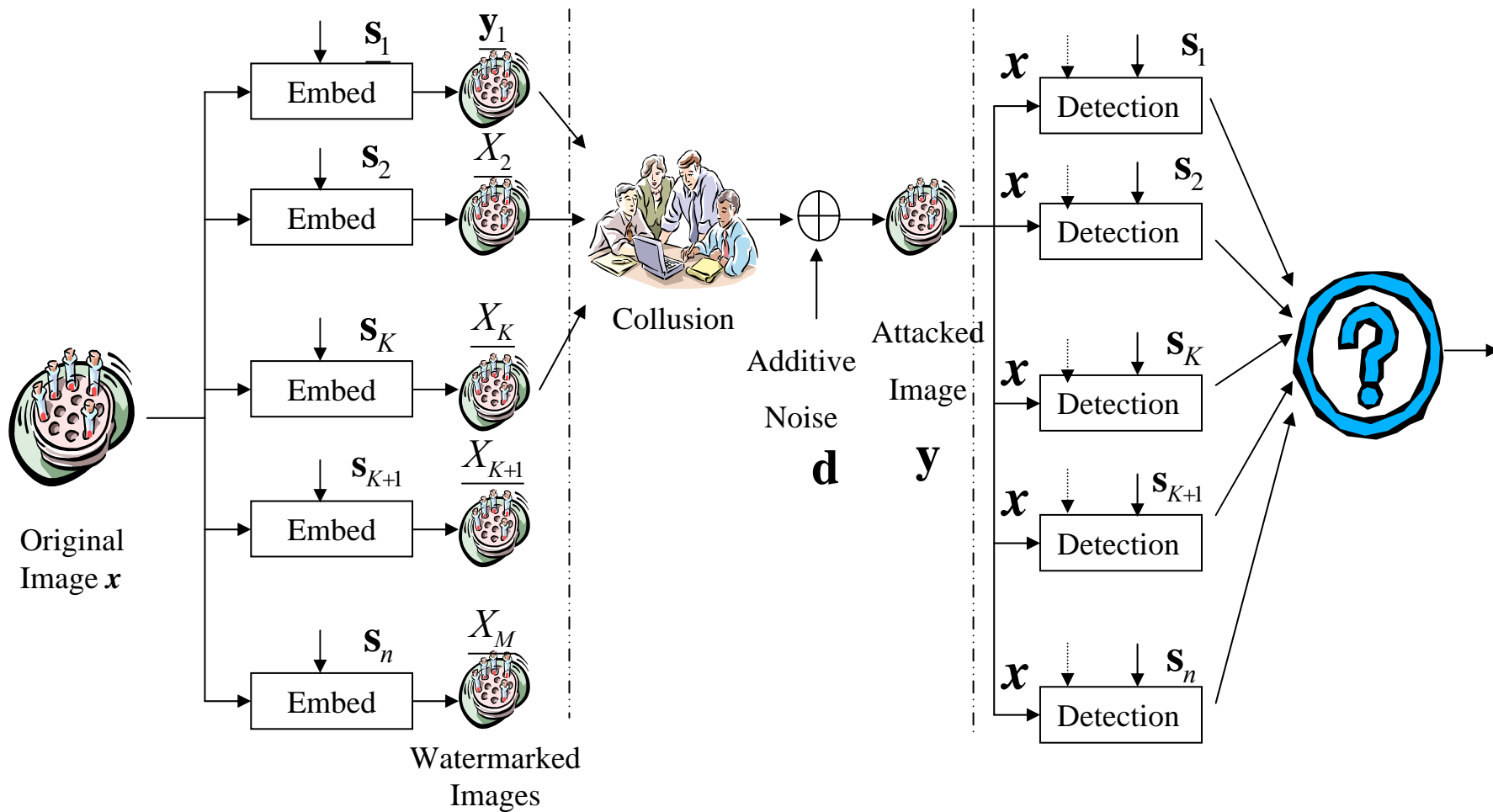
<http://www.msnbc.msn.com/id/4037016/>



# Embedded Fingerprinting for Multimedia



# Model



# Modulation Scheme for Embedded Fingerprinting

- Typical watermark-to-noise (WNR) ratio: -20dB in blind detection, 0dB in non-blind detection.
- Choice of modulation schemes:

Orthogonal modulation  $\mathbf{s}_j = \mathbf{u}_j$

# of fingerprints  
= # of ortho. bases

(Binary) coded modulation  $\mathbf{s}_j = \sum_{i=1}^v b_{ij} \mathbf{u}_i$

for  $b_{ij} \in \{0,1\}$  or  $b_{ij} \in \{\pm 1\}$

# of fingerprints  $\gg$  # of ortho. bases





# Performance Criteria

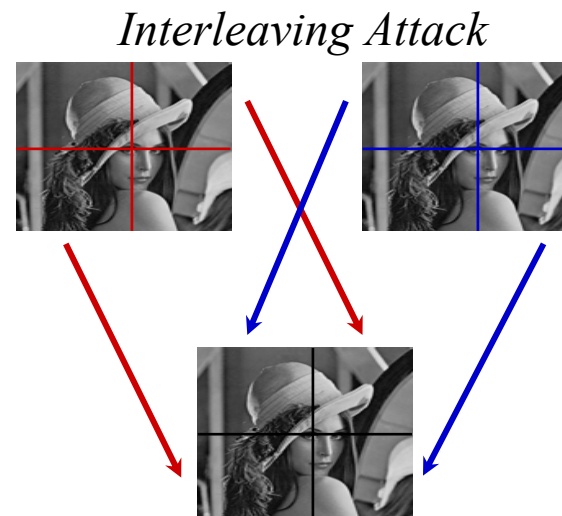
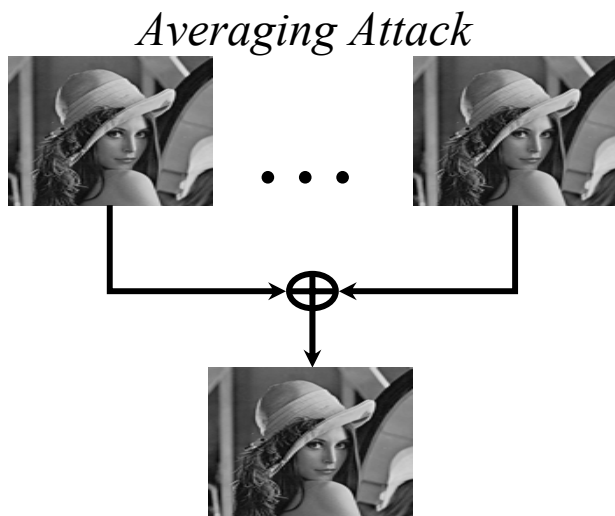
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- **Capture one:** The major concern is to identify at least one colluder with high confidence without accusing innocent users.
- **Capture more:** The major concern is to catch more colluders, possibly at a cost of accusing more innocents. Tradeoff between the expected fraction of colluders that are successfully captured and the expected fraction of innocent users that are falsely placed under suspicion.
- **Capture all:** The goal is to capture all colluders with a high probability. Tradeoff between the efficiency rate which describes the amount of expected innocents accused per colluder and the probability of capturing all colluders.



# Collusion Attacks by Multiple Users

- Collusion: A cost-effective attack against multimedia fingerprints
- Result of fair collusion:
  - Each colluder contributes equal share through averaging, interleaving, and nonlinear combining
  - Energy of embedded fingerprints may decrease



# Collusion Attacks (cont'd)

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- Though linear collusion is simple and effective, in fact, for each component, **the colluders can output any value between the minimum and maximum values**, and have high confidence that such spurious value is within the range of JND. Therefore,

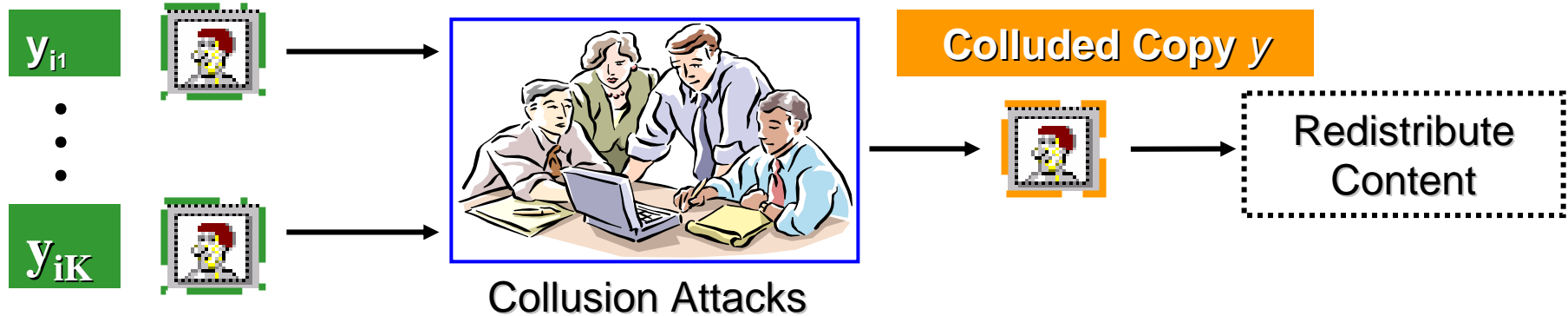
*We conduct studies on non-linear attacks*

- Few previous works: H. Stone suggested several nonlinear collusion attacks

 *What is the best attack for collusions?*



# Nonlinear Collusion Attacks



- **Assumption**

- Colluders pick value in the range of min and max of  $\{y_j(i)\}_{j \in S_C}$
- FP embedding and collusion attack are in the same domain

- **Order statistics based collusion:** for each component  $i$ ,  $i=1, \dots, N$ ,

$$y(i) = x(i) + \alpha \cdot JND(i) \cdot g(s_j(i))_{j \in S_C}$$

$$V(i)^{ave}; V(i)^{\min}; V(i)^{\max}; V(i)^{median}$$

$$V(i)^{\min \max} = average(V(i)^{\min}, V(i)^{\max})$$

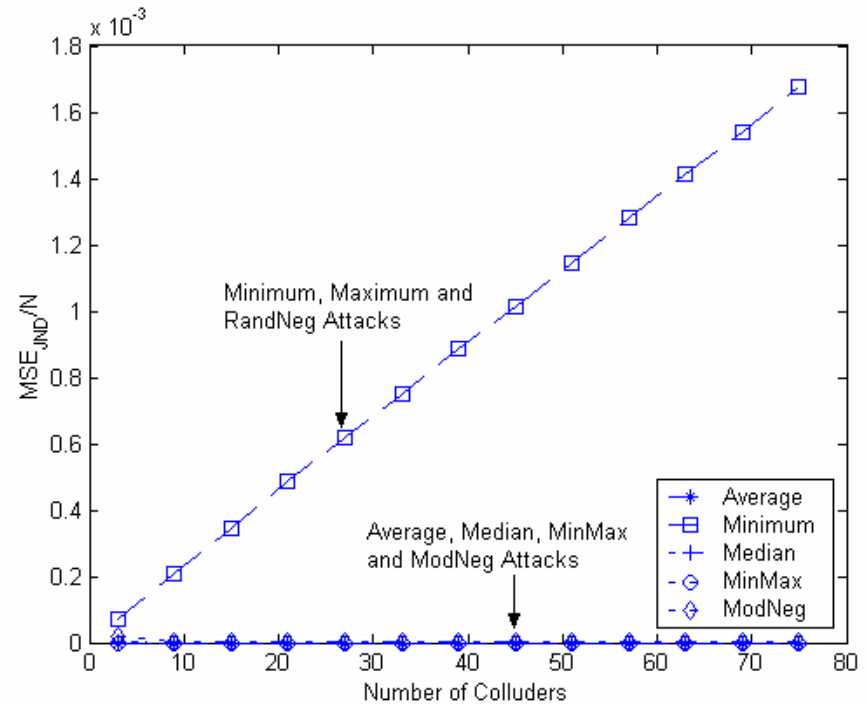
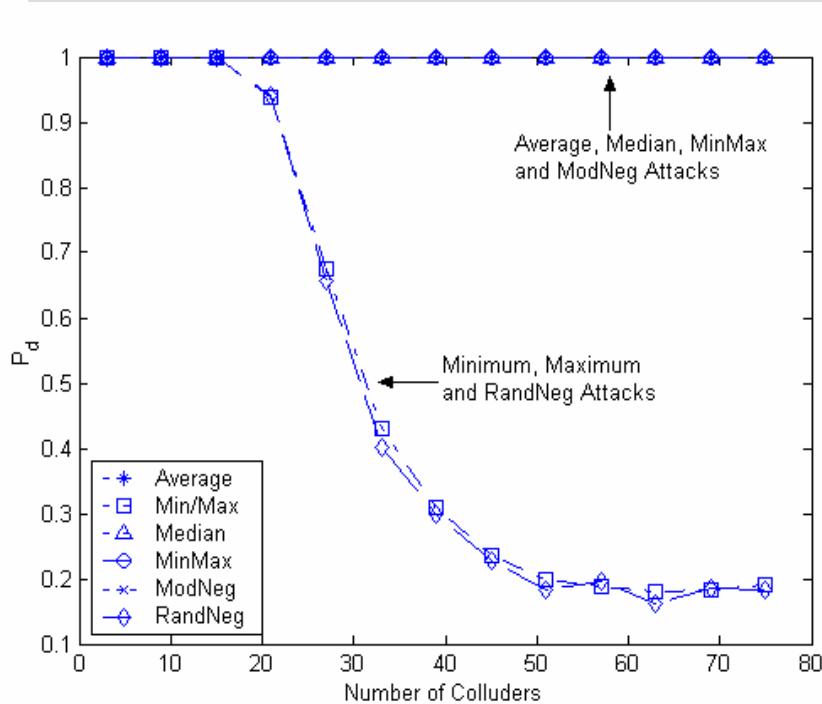
$$V(i)^{mod \ neg} = V(i)^{\min} + V(i)^{\max} - V(i)^{med}$$

$$V(i)^{rand \ neg} = \begin{cases} V(i)^{\min} & \text{w.p. } p \\ V(i)^{\max} & \text{w.p. } 1 - p \end{cases}$$

$p=0.5$  in randomized negative attack and is indep. of  $\{s(i)\}$



# Example: use $T_n$ Statistic



- Assume the host signal has  $N=10,000$  embeddable coefficients and there are a total of  $n=100$  users.  $P_{fp}=10^{-3}$  is fixed and i.i.d. fingerprints  $\sim N(0,1/9)$ .
- **Randomized negative attack** is the most effective attack (without normalizing the distortion level introduced by different attacks).
- **Minimum, maximum and randomized negative attacks** introduce much larger distortion in the colluded copy



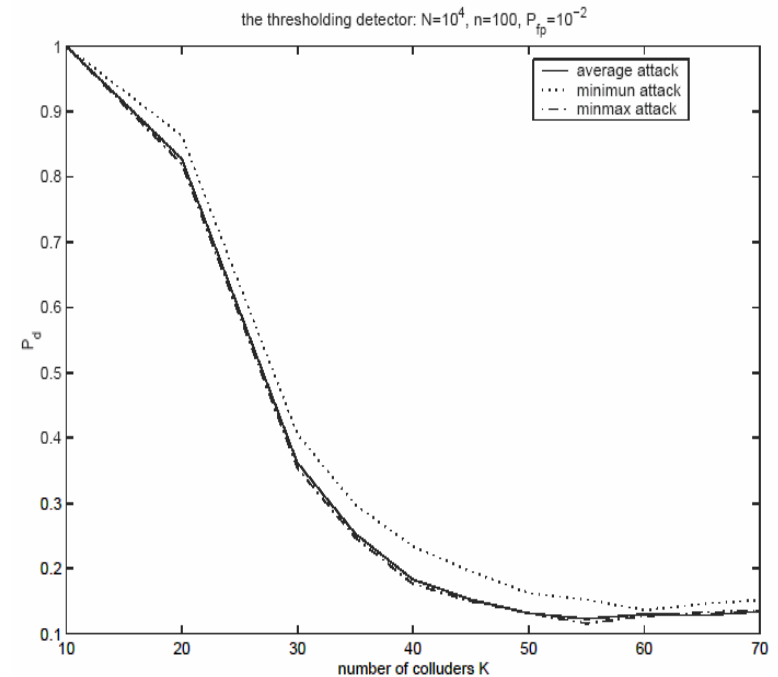
# Averaging and Nonlinear Collusions (cont'd)

Thresholding detector is robust to different types of attacks:  
*averaging collusion; order-statistic based (min, max, ...)*

## Rationale from detector's view point

Detection statistics of averaging and many nonlinear collusions are (approx.) Gaussian distributions with same mean

⇒ Yield similar performance if the overall distortion is the same.



$$g(\mathbf{s}_j, j \in S_c) + \mathbf{d}_1$$



nonlinear attacks

$$\frac{1}{K} \sum_{j \in S_c} \mathbf{s}_j + \mathbf{d}_2$$



average attacks



# Linear vs. Nonlinear Collusion

- **Conditions:** - distortion introduced to the host signal is equal
- **Observation:** the underline model of attacks doesn't matter much from the detector point of view.
- **All types of attacks can be modeled as attacks by averaging:** the models

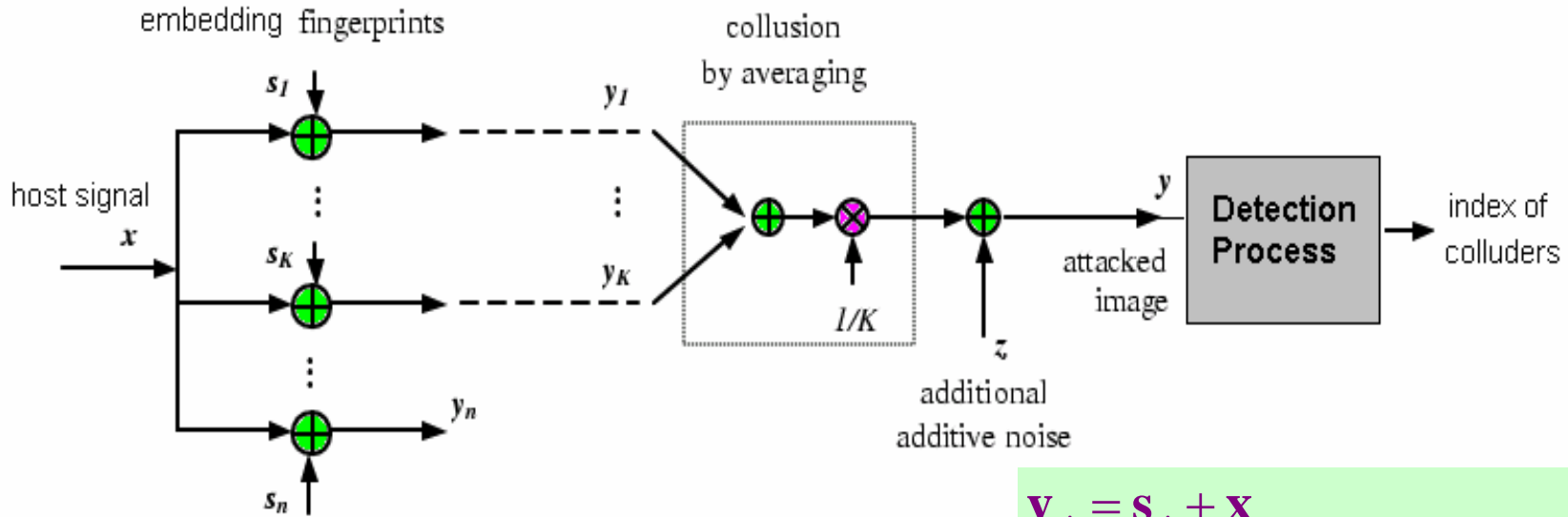
$$\mathbf{y}_1 = g(\mathbf{s}_j, j \in S_c) + \mathbf{d}_1 \rightarrow \text{nonlinear attacks}$$
$$\mathbf{y}_2 = \frac{1}{K} \sum_{j \in S_c} \mathbf{s}_j + \mathbf{d}_2 \rightarrow \text{average attacks}$$

yield similar performance. The detector is robust to different types of attacks.

*We shall focus on average attack for analysis simplicity*



# Average Attack



$$\mathbf{y} = \frac{1}{K} \sum_{j \in S_c} \mathbf{y}_j + \mathbf{z} = \frac{1}{K} \sum_{j \in S_c} \mathbf{s}_j + \mathbf{d}$$

$$\mathbf{y}_j = \mathbf{s}_j + \mathbf{x}$$

$$d(i) \sim N(0, \sigma_d^2), \text{ for } i = 1, \dots, N.$$

$$\mathbf{s}_j \perp \mathbf{s}_k, \forall j \neq k$$

$$WNR: \eta = \|\mathbf{s}\|^2 / \|\mathbf{d}\|^2$$

**Problem:** determine the number of colluders  $K$  and the subset  $S_c$



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# ***Orthogonal Modulation for Fingerprinting***



# Orthogonal Fingerprinting

- **Straightforward concept and easy to implement**
    - Prior works by Cox et al., Stone, Killian et al.
    - Advantage in distinguishing individual fingerprints
  - **Two issues limit the anti-collusion capability:**
    - Orthogonal fingerprints get attenuated with more colluders
      - leads to reduced detection statistics corresponding to colluders
    - Probability of false alarm increases as the total # of users increases
  - **Tracing Capability:** How many colluders out of how many users are sufficient to break down a fingerprinting system?
  - **To meet desired probability of detection ( $P_d$ ) & false alarm ( $P_{fp}$ )**
    - We can analyze the maximum allowable colluders
- ⇒ This provides design guidelines to fingerprinting systems for applications with different protection requirements



# Formulations for Max. Number of Colluders

- Thresholding detector:  
(index of colluders)

$$\hat{\mathbf{j}} = \arg \max_{j=1,\dots,n} \{T_N(j) \geq h\}$$

- Performance criteria:  
(Catch one: )

$$P_{fp} = P_r \{\hat{\mathbf{j}} \cap \bar{S}_c \neq \emptyset\} = 1 - (1 - Q(h / \sigma_d))^{n-K}$$
$$P_d = P_r \{\hat{\mathbf{j}} \cap S_c \neq \emptyset\} = 1 - (1 - Q(\frac{h - \|s\| / K}{\sigma_d}))^K$$

- System requirement:

$$\begin{matrix} P_{fp} \leq \varepsilon \\ P_d \geq \beta \end{matrix} \longrightarrow K_{\max}$$

- The desired  $P_{fp}$  determines the threshold for the detector
- The desired  $P_d$  determines the maximum # of colluders allowed by the fingerprinting system



# Bounds for Max. Number of Colluders

- Lower bound and Upper bound for  $K_{\max}$ 
  - Obtained by analytic approximations on Q-functions

$$K_{\max} \geq \min\{n, K_L\}, \text{ where } K_L = \frac{\sqrt{\eta N}}{h_H} = \sqrt{\frac{\eta N}{\log(n^2 / (2\pi\epsilon^2 \log(2\pi n^2)))}} \sim \sqrt{\frac{\eta N}{\log(n)}}$$

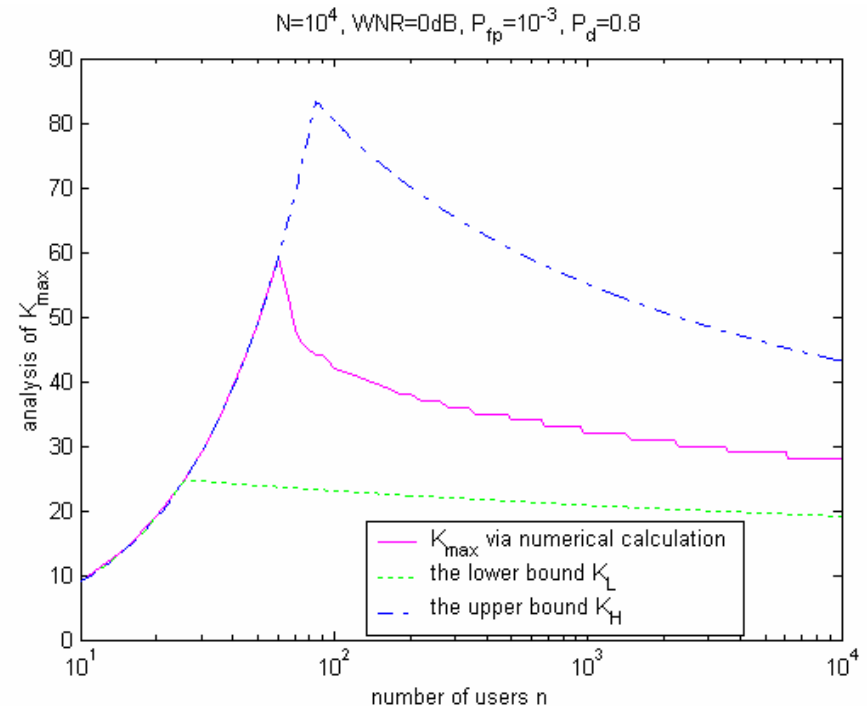
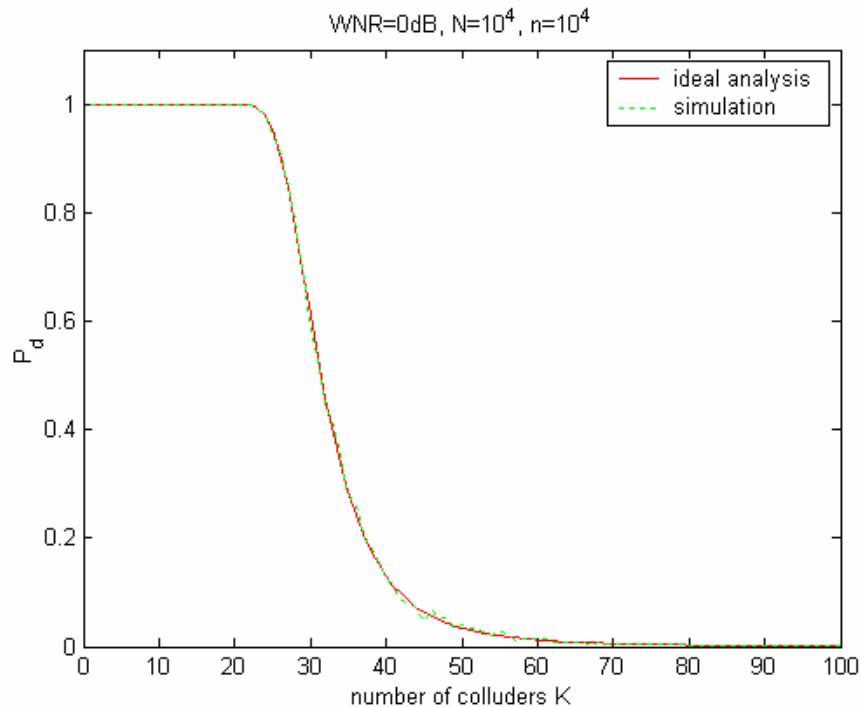
$$K_{\max} \leq \min\{n, K_H\}, \text{ where } K_H = \frac{\sqrt{\eta N}}{h_L - Q^{-1}(1 - \tilde{K}\sqrt{1 - \beta})}$$

- two auxiliary variables are defined as

$$h_L = \sqrt{\log(2\pi n^2)}$$
$$\tilde{K} = \frac{\sqrt{\eta N}}{h_L - Q^{-1}(1 - \sqrt{1 - \beta})}$$



# Results



- Stringent requirement: correct identification of at least one colluders without falsely accusing any
- The colluder tracing capabilities for a thousand-user system is limited to several dozens colluders



# Different Performance Criteria

- Catch more

the expected fraction of innocents falsely suspected:  $r_i = Q(h / \sigma_d)$

the expected fraction of colluders successfully captured:  $r_c = Q\left(\frac{h - \|\mathbf{s}\| / K}{\sigma_d}\right)$

- Catch all

$R = \frac{\text{the expected number of innocents captured}}{\text{the expected number of colluders captured}}$

$P_d = P_r(S_c \subseteq \hat{\mathbf{j}})$

Different sets of performance criteria were studied. It seems that an orthogonal fingerprinting system can resist to the collusion attacks based on a few dozen independent copies.



# Group-Oriented Forensics

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- Overcome the limitations of orthogonal fingerprinting
  - Recall: orthogonal FP treats everybody equally
- Colluders often come together in some foreseeable groups
  - Due to their geographic, social, or other connections
- Our approach: design users' FP in a correlated way
  - Cluster users into groups based on prior knowledge
    - ◆ *Intra-group collusion is more likely than inter-group*
- Design of collusion-resistant fingerprinting systems:
  - Design of anti-collusion fingerprints to trace traitors and colluders
  - Design of detection schemes

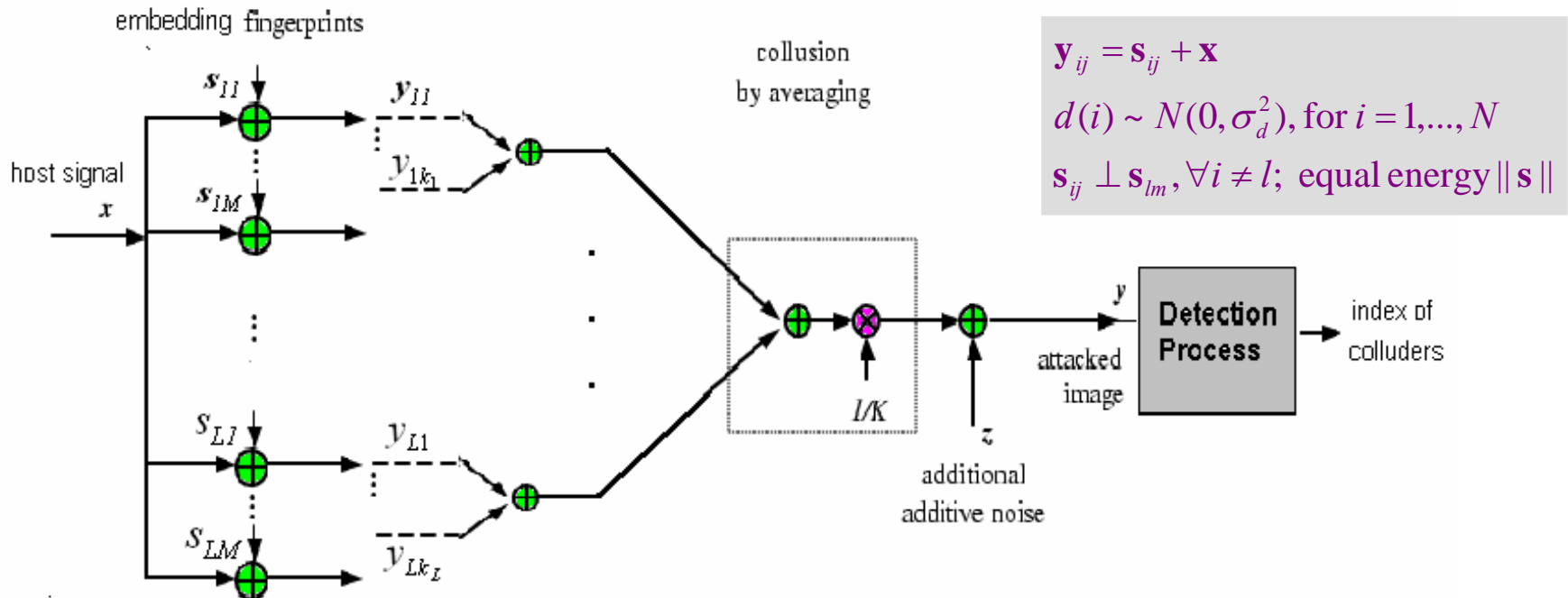




# Proposed Group Fingerprinting

## Design of collusion-resistant fingerprinting systems:

- Design of anti-collusion fingerprints to trace traitors and colluders
- Design of detection schemes



**Solution:** construct intra-group FP in two parts, and use threshold detector (at desired intra-group false alarm) to avoid estimating  $k_i$



# Group Fingerprint Design

- Orthogonal modulation between groups
  - Design  $L$  orthogonal sub-systems to represent independent groups
  - $M$  users per group  $\Rightarrow$  Total:  $n = M \times L$  users
- Assumption: users in the same group are equally likely to collude with each other.

- Real-valued code modulation within a group

- Introduce equal correlation within a group

$$\mathbf{S} = [\mathbf{s}_{i1}, \mathbf{s}_{i2}, \dots, \mathbf{s}_{iM}]$$

the correlation matrix of  $\{\mathbf{s}_{i,j}\}$  is  $\mathbf{R}_s$

$$\mathbf{R}_s = \begin{bmatrix} 1 & \rho & \dots & \rho \\ \rho & 1 & \ddots & \vdots \\ \vdots & \ddots & \ddots & \rho \\ \rho & \dots & \rho & 1 \end{bmatrix}$$

- Each fingerprint consists of common one and individual one:

$$\mathbf{s}_{ij} = \sqrt{1-\rho}\mathbf{e}_{ij} + \sqrt{\rho}\mathbf{a}_i, \text{ where } \{\mathbf{e}_{i1}, \dots, \mathbf{e}_{iM}, \mathbf{a}_i\} \sim iid N(0, \sigma_u^2 \mathbf{I}_N)$$



# Two-Stage Detection Scheme

- Basic idea: first identify groups containing colluders, then identify colluders with each possible guilty group
- Stage-1: group detection

$$\hat{\mathbf{i}} = \arg_{i=1}^L \{T_G(i) \geq h_G\} \quad (\text{the indices of groups})$$

$$\text{the correlator } T_G(i) = \frac{(\mathbf{y} - \mathbf{x})^T (\mathbf{s}_{i1} + \mathbf{s}_{i2} + \dots + \mathbf{s}_{iM})}{\sqrt{\|\mathbf{s}\|^2 [M + (M^2 - M)\rho]}}, \text{ for } i = 1, \dots, L$$

$$p(T_G(i) | K, \{k_i\}, \sigma_d^2) = \begin{cases} N(0, \sigma_d^2), & \text{if } k_i = 0 \\ N\left(\frac{k_i}{K} \|\mathbf{s}\| r, \sigma_d^2\right), & \text{o.w.} \end{cases}$$

$$r = \sqrt{[1 + (M - 1)\rho] / M}$$



# Two-Stage Detection Scheme (cont'd)

- Stage-2: Identify colluders within each group

Define the correlator:  $T_{ei}(j) = \frac{\sqrt{1-\rho}(\mathbf{y}-\mathbf{x})^T \mathbf{e}_{ij}}{\|\mathbf{s}\|}$ , for  $i=1, \dots, L$



$$\hat{\mathbf{j}}_i = \arg \max_{j=1}^M \{T_{ei}(j) \geq h\}$$

(the indices of colluders within group  $i$ )

$h$  does not depend on  $i$

$$p(\mathbf{T}_{ei} | K, S_{ci}, \sigma_d^2) = N(\boldsymbol{\mu}_{ei}, \sigma_d^2 \mathbf{I}_M),$$

with  $\mu_{ei}(j) = \begin{cases} \frac{1-\rho}{K} \|\mathbf{s}\|, & \text{if } j \in S_{ci} \\ 0, & \text{o.w.} \end{cases}$

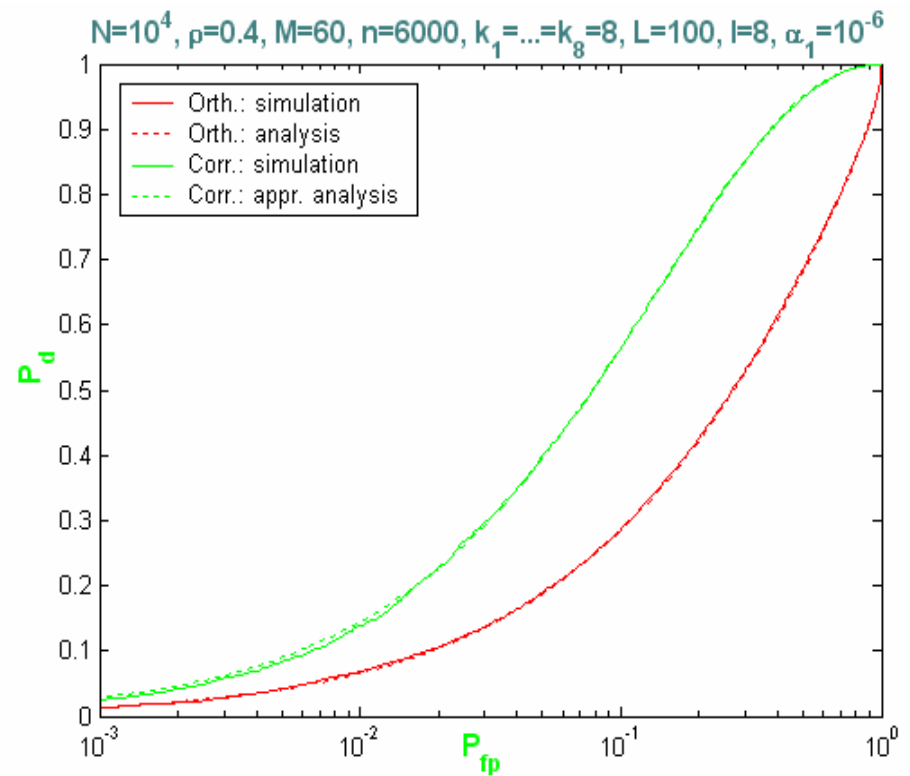
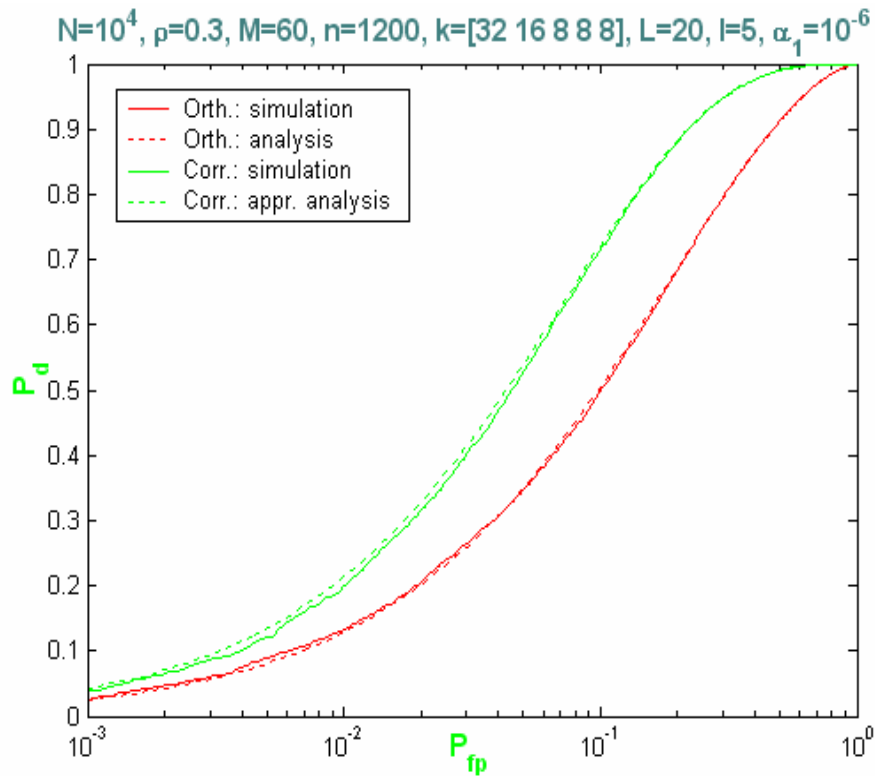
$T_{ei}(j)$ 's are independent



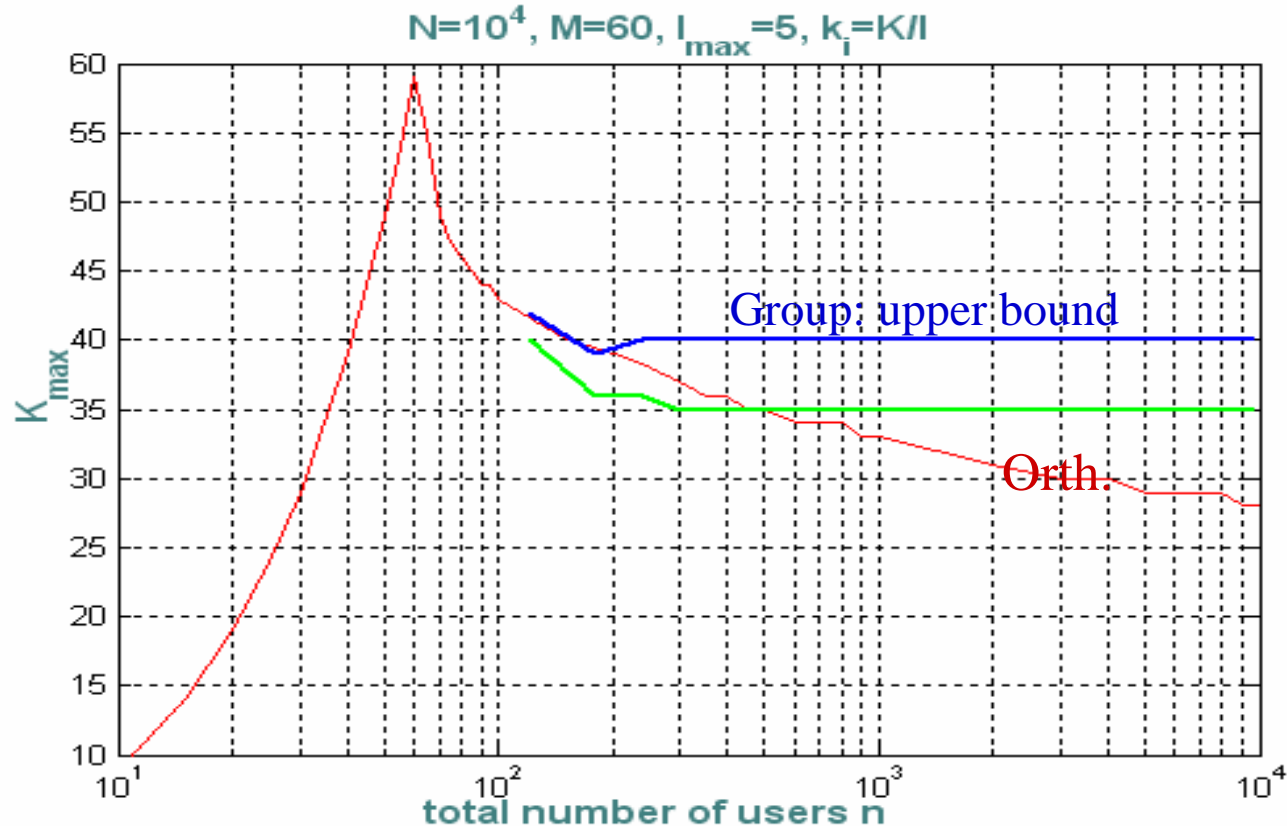
# Example:

ROC Curves  $P_d$  vs.  $P_{fp}$  under different collusion settings

Constraint: equal energy  $E\{\|\mathbf{y}_c\|^2\} = E\{\|\mathbf{y}_0\|^2\} \equiv \|\mathbf{s}\|^2$



# Collusion Resistance of Group FP: $K_{\max}$ vs. $n$



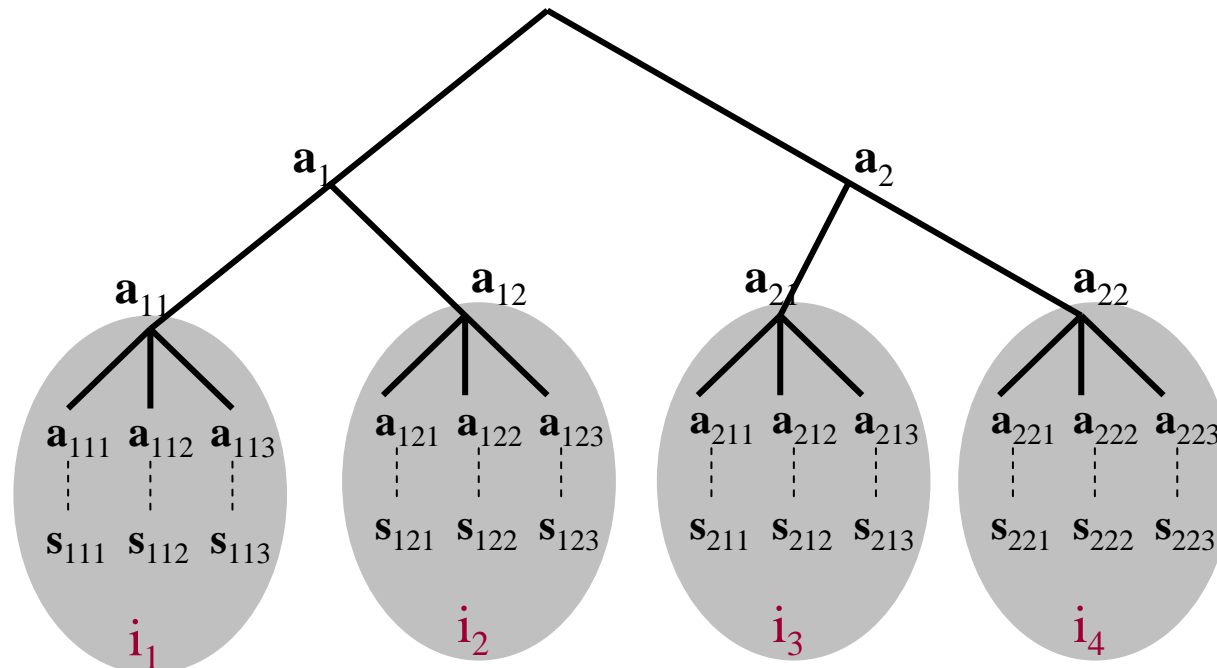
$$P_{fp} \leq 10^{-3}$$
$$P_d \geq 0.8$$

- $K_{\max}$  of the proposed scheme is larger than that of the orthogonal scheme (the solid line), when  $n$  is large.
- Difference between the lower bound and upper bound is due to the fact that  $k_i=K/l_i$  in our simulations (symmetric collusion pattern).
- The smaller the number of guilty groups, the better chance performance.



# Extension: Tree-based Fingerprint Design

- Use **tree structure** to construct fingerprints combining shared and distinct components
- Unified view of fingerprint construction using code modulation
  - With hierarchically organized basis vectors
  - Allow for real-valued codes



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# ***Coded Modulation for Fingerprinting***



# Coded Fingerprinting: Prior Work and New Issues

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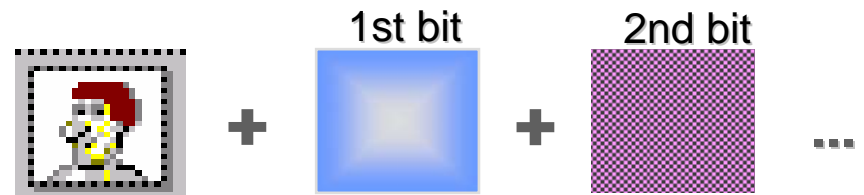
- Collusion-secure codes by Boneh and Shaw '98
  - Targeted at generic data with “Marking assumptions”
    - ~ *an abstraction of collusion model*
  - Codes are too long to be reliably embedded & extracted (Su et al.)
    - ~ *millions bits for 1000 users*
  - Focus on tracing one of the colluders
- New issues with multimedia
  - “Marking assumptions” may no longer hold ...
  - Some code bits may become erroneously decoded due to strong noise and/or inappropriate embedding
  - Can choose appropriate embedding to prevent colluders from arbitrarily changing the embedded fingerprint bits
- Want to trace as many colluders as possible



# Spreading + Combinatorial Coded Fingerprinting

- Overall idea of embedded combinatorial fingerprinting
  - Explore unique issues associated with multimedia in fingerprint encoding, embedding & detection
  - Use appropriate embedding to prevent arbitrary change on code

$$\mathbf{w}_j = \sum_{i=1}^B b_{ij} \mathbf{u}_i \quad b_{ij} \in \{\pm 1\}$$



- Build correlated fingerprints in two steps
  - Binary Anti-collusion fingerprint codes resist up to  $K$  colluders
    - ◆ *any subset of up to  $K$  users share a unique set of code bits*
  - Use antipodal coded modulation to embed fingerprint codes
    - ◆ *via orthogonal spread spectrum sequences*
    - ◆ *shared bits get sustained and used to identify colluders*

# 16-bit ACC for Detecting $\leq 3$ Colluders Out of 20

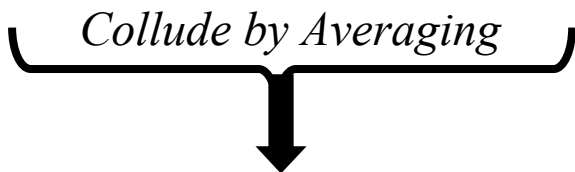
User-1 ( **-1,-1, -1, -1, 1, 1, 1, 1, ..., 1** )



( **-1, 1, 1, 1, 1, 1, ..., -1, 1, 1, 1** ) User-4



Embed fingerprint via HVS-based spread spectrum embedding in block-DCT domain



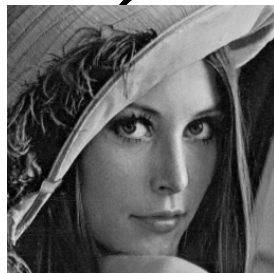
Uniquely Identify User 1 & 4

Extracted fingerprint code ( **-1, 0, 0, 0, 1, ..., 0, 0, 0, 1, 1, 1** )



# ACC Codes Under Averaging Collusion

User 1:	-1	-1	-1	-1	1	1	1	1	1	1	1	1	1	1	1
User 4:	-1	1	1	1	1	1	1	1	1	-1	-1	-1	1	1	1
User 8:	1	-1	1	1	1	1	-1	1	-1	1	1	1	1	-1	1
User(1,4) Average:	-1	0	0	0	1	1	1	1	1	0	0	0	1	1	1
User(1,4,8) Average:	$-\frac{1}{3}$	$-\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	1	1	$\frac{1}{3}$	1	$\frac{1}{3}$	1	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	1	$\frac{1}{3}$
After thresholding:	0	0	0	0	1	1	0	1	0	1	0	0	0	1	0



User-1



User-4



User-8

- Averaging of multimedia domain leads to averaging in code-domain, and corresponds to AND operation after thresholding
- Can distinguish colluded bits from sustained bits statistically with appropriate modulation and embedding, and the sustained bits are unique with respect to colluder set

# Anti-Collusion Codes (ACC)

- ACC code via combinatorial design

- Balanced Incomplete Block Design (BIBD)

## Simple Example

ACC code via (7,3,1) BIBD for handling up to 2 colluders among 7 users

$$C = \begin{pmatrix} 0 & 0 & 1 & 0 & 1 & 1 & 1 \\ 0 & 1 & 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 1 & 1 & 0 & 1 & 0 \\ 1 & 0 & 0 & 1 & 0 & 1 & 1 \\ 1 & 0 & 1 & 1 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 & 1 & 1 & 0 \\ 1 & 1 & 1 & 0 & 0 & 0 & 1 \end{pmatrix}$$

- (v,k,λ)-BIBD is an (k-1)-resilient AND ACC

- Defined as a pair (X,A)

- ◆ X is a set of v points
- ◆ A is a collection of blocks of X, each with k points
- ◆ every pair of distinct points is in exactly λ blocks

- # blocks  $n = \frac{\lambda(v^2 - v)}{k^2 - k}$

- Code length for n=1000 users:  $O(n^{0.5}) \sim$  dozens-to-hundreds bits

- Shorter than prior art by Boneh-Shaw  $O((\log n)^6) \sim$  millions bits



# Colluder Detectors

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- **Hard Detection:**

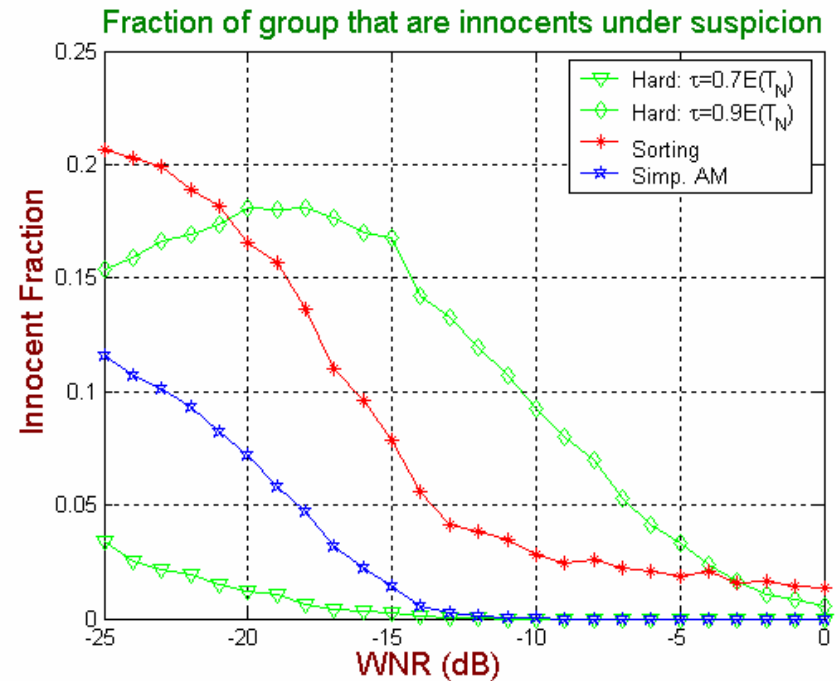
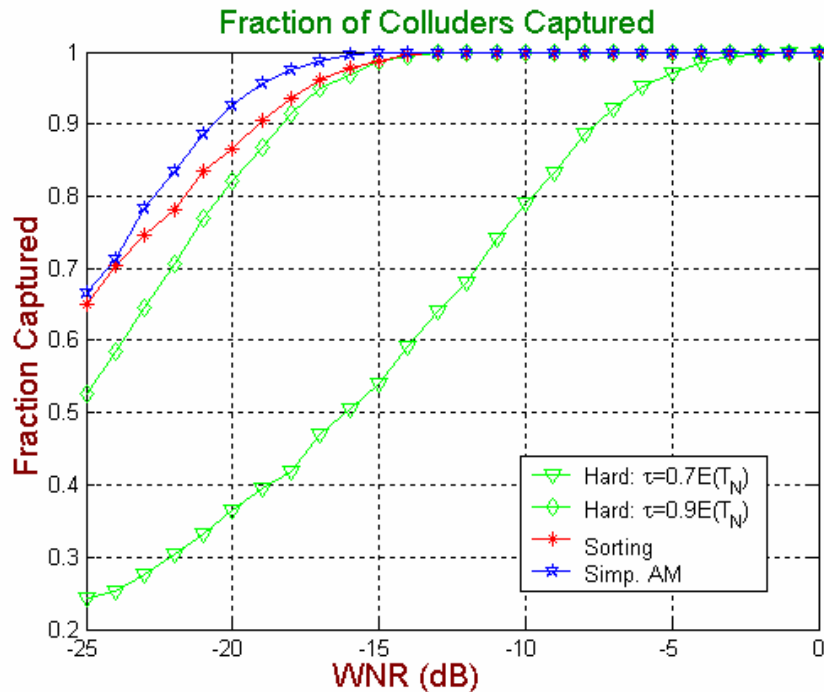
- Detect the bit values and **then** estimate colluders from these values
- Uses the fact that the combination of codevectors uniquely identifies colluders
- Everyone is suspected as guilty and each ‘1’ bit narrows down set

- **Soft Detection:**

- Possible candidates for soft detection:
  - ◆ *Sorting: Use the largest detection statistics to optimize likelihood function to **first** determine bit values, **then** estimate colluder set.*
  - ◆ *Sequential: Iteratively update the likelihood function and **directly** identify the colluder set.*



# ACC Experiment with Gaussian Signals



- Higher threshold captures more colluders, but suspects more innocents
- Soft decoding gives more accurate colluder identification than hard decoding
- Joint decoding and colluder identification gives better performance than separating the two steps





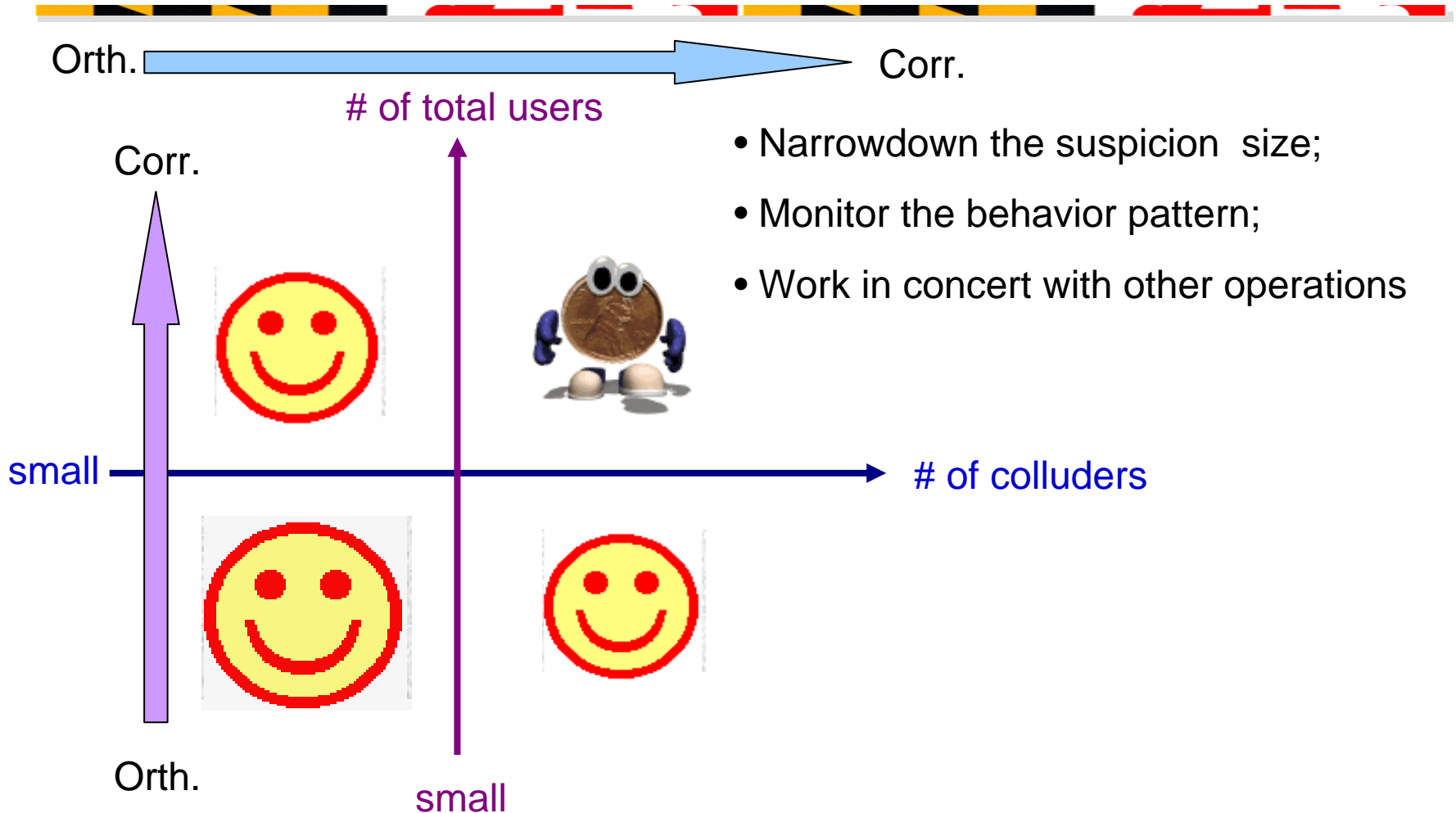
# Summary

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- Important to design anti-collusion fingerprint for multimedia
  - Collusion is a cost-effective attack against fingerprinting
  - Anti-collusion fingerprint can allow us to trace traitor and deter unauthorized information leakage
- Good news
  - We can tolerate about a few dozens colluders
  - We can accommodate more users through the ACC
- Challenge
  - One can find enough colluders to circumvent the system



# Conclusions (cont'd)



- So we have more work do... tomorrow will be better!



# ***Traitors Behavior Dynamics in Collusion***



# ***Fairness Issue in Collusion***

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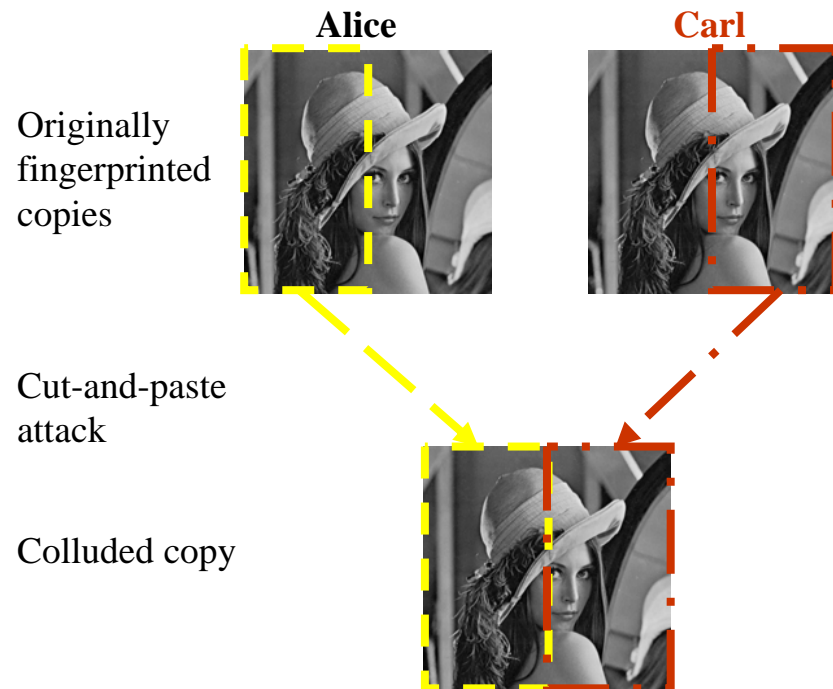
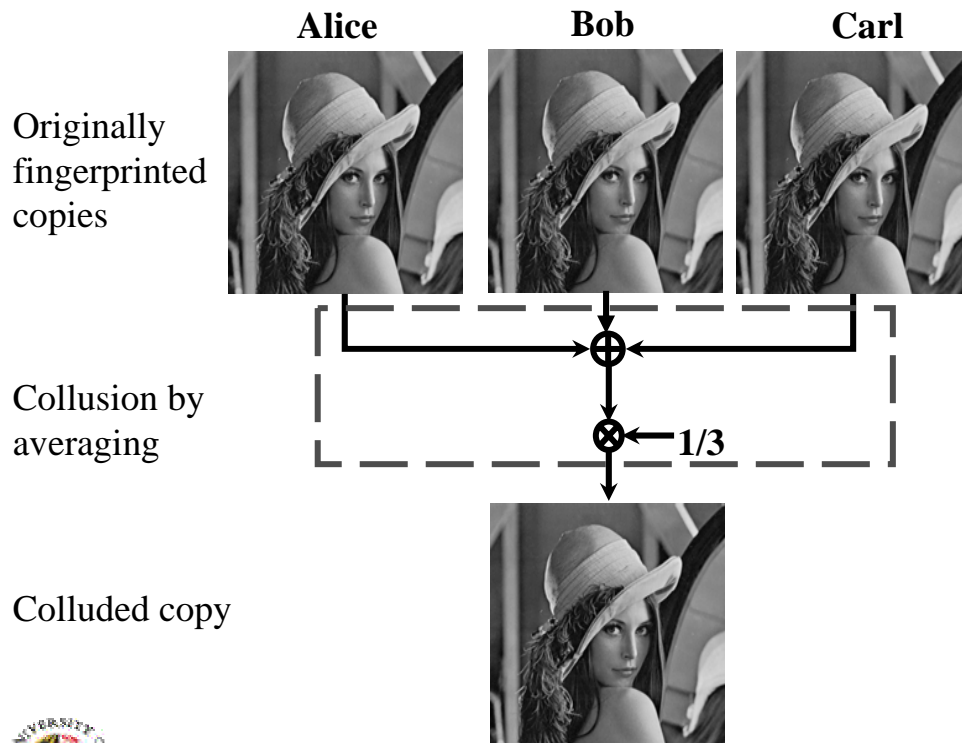
- **Multi-user collusion**
  - Colluders share the profit as well as the risk of being caught
- **Fairness issue in collusion**
  - All colluders have the same probability of being detected
- **Each colluder ensures that he/she is not taking higher risk of being detected than the others**

➤ **Fair-play during collusion**



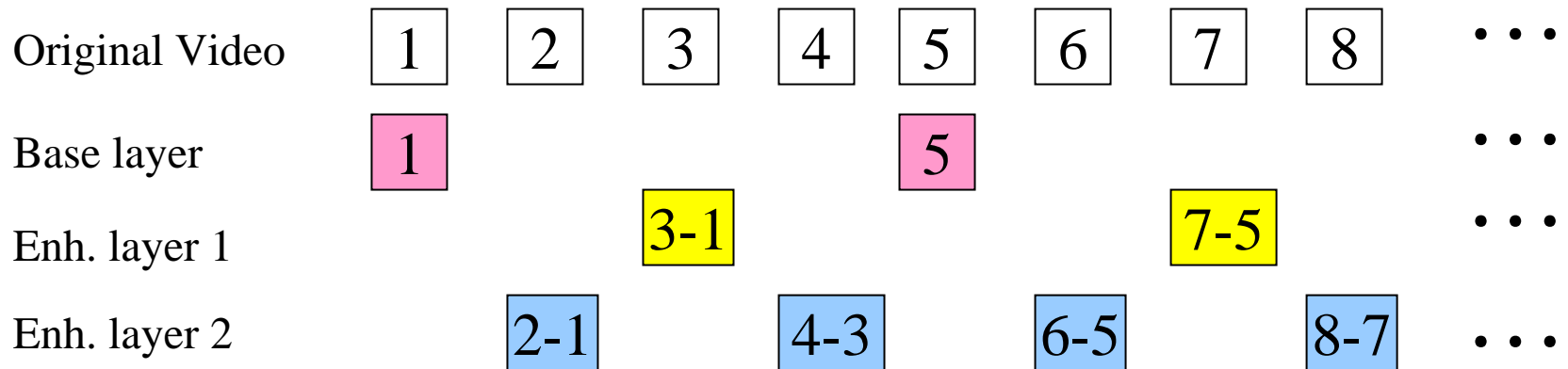
# Achieving the Fairness of Collusion

- Prior work: all users receive copies of the same quality
  - Examples of fair collusion: averaging, cut-and-paste
  - Reduces the energy of each contributing fingerprint by an equal ratio

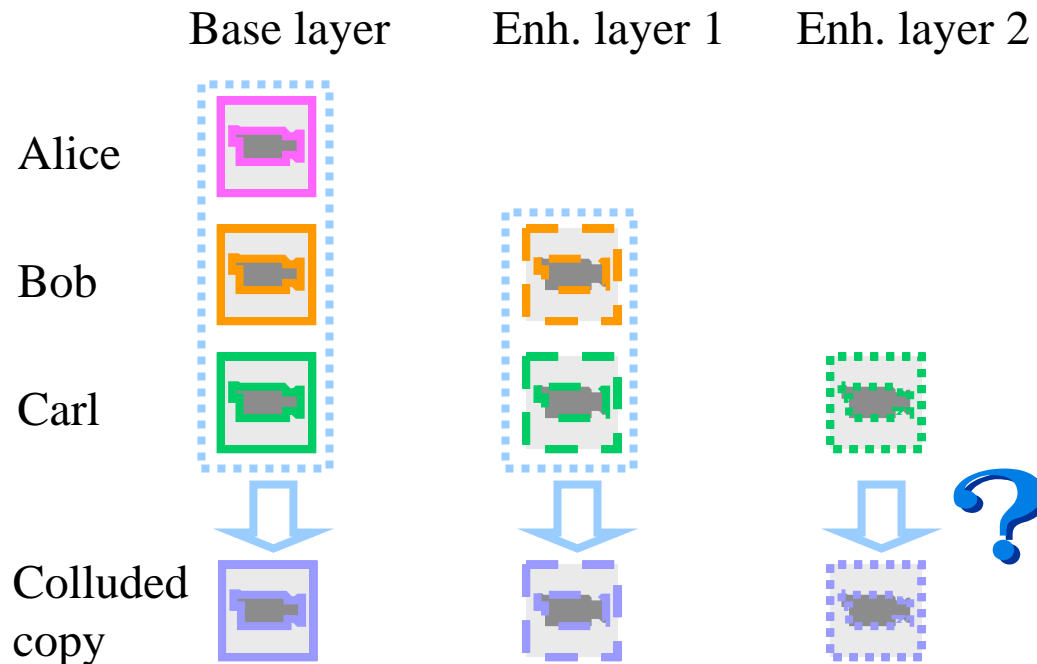


# Achieving the Fairness of Collusion (cont'd)

- Scalable multimedia coding: network and device heterogeneity
  - Users receive copies of different quality
  - Temporal scalability: multiple versions of the same video with different frame rates
  - Layered coding: decompose the video into non-overlapping bit streams of different priorities

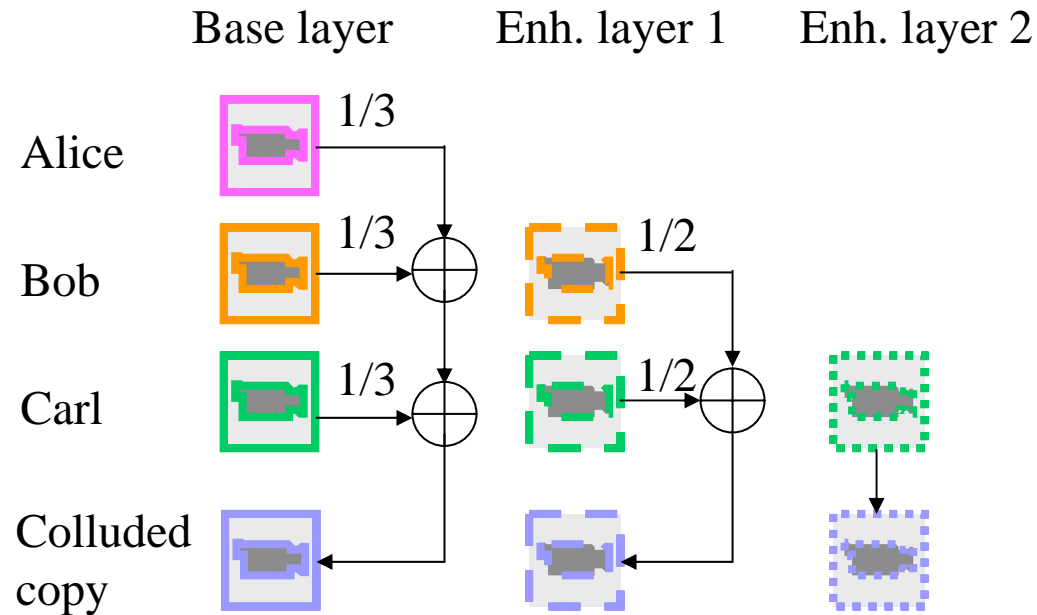


# Achieving the Fairness of Collusion (cont'd)



**Problem:** how to achieve the fairness of collusion in scalable fingerprinting systems?

# Achieving the Fairness of Collusion (cont'd)



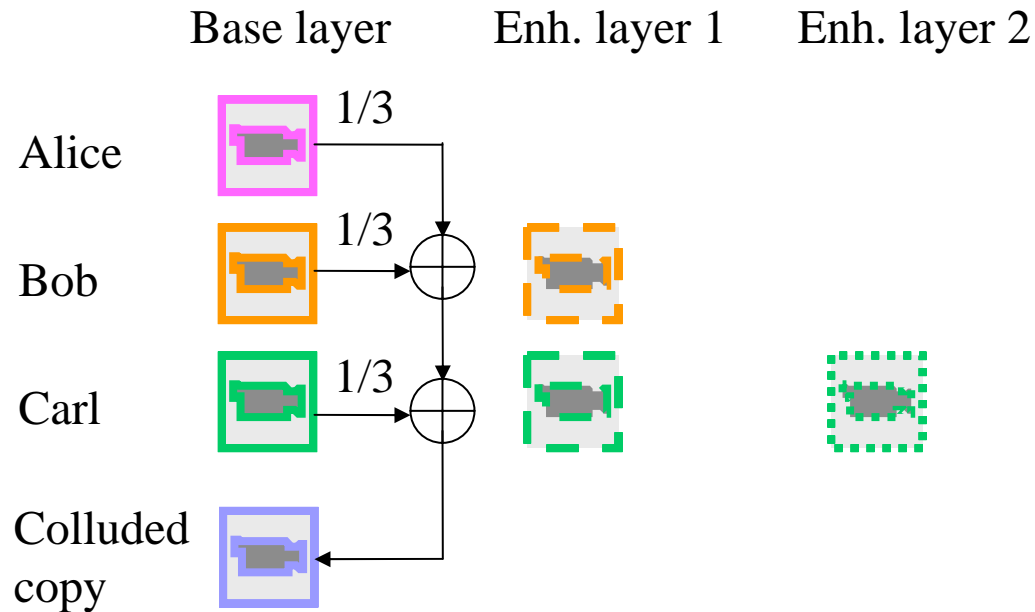
Quality of the colluded copy    High

Probability of being detected     $P_{\text{Carl}} > P_{\text{Bob}} > P_{\text{Alice}}$





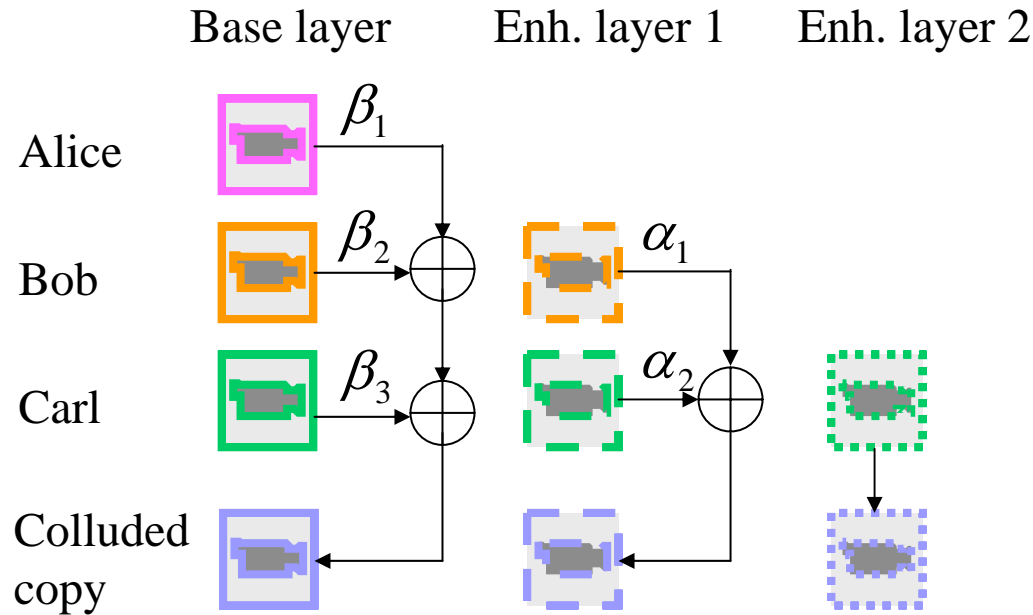
# Achieving the Fairness of Collusion (cont'd)



Quality of the colluded copy **Low**

Probability of being detected  $P_{\text{Carl}} = P_{\text{Bob}} = P_{\text{Alice}}$

# Achieving the Fairness of Collusion (cont'd)



Quality of the colluded copy      High

Probability of being detected       $P_{\text{Carl}} = P_{\text{Bob}} = P_{\text{Alice}}$

➤ Choose  $\{\alpha, \beta\}$  to guarantee the equal risk of all colluders

# Analysis of Each Colluder's Risk

- Consider a simple detector that uses fingerprints extracted from all layers collectively to identify colluder.
- The correlation based detection statistics:  $T_N^{(i)} \sim N(\mu^{(i)}, \sigma_n^2)$ 
  - For different users,  $T_N^{(i)}$  have the same variance  $\sigma_n^2$  but different means  $\mu^{(i)}$
- To achieve the fairness of collusion, seek  $\{\beta_k\}$  and  $\{\alpha_l\}$  such that  $\mu^{(i)}$  are the same for all colluders.

$$\begin{aligned} \mu^{(Alice)} &= \mu^{(Bob)} = \mu^{(Carl)} \\ \text{s.t. } 0 &\leq \beta_1, \beta_2, \beta_3 \leq 1, \beta_1 + \beta_2 + \beta_3 = 1 \\ 0 &\leq \alpha_1, \alpha_2 \leq 1, \alpha_1 + \alpha_2 = 1 \end{aligned}$$



# Fairness Issue During Collusion

$F^c = F_b \cup F_{e1} \cup F_{e2}$ (Highest resolution)	Fairness Constraints	$\begin{cases} \frac{K^b \sqrt{N_b}}{K^b \sqrt{N_b} + K^{b,e1} \sqrt{N_b + N_{e1}} + K^{all} \sqrt{N_b + N_{e1} + N_{e2}}} \leq \frac{N_b}{N_b + N_{e1} + N_{e2}}, \\ \frac{K^{all} \sqrt{N_b + N_{e1} + N_{e2}}}{K^b \sqrt{N_b} + K^{b,e1} \sqrt{N_b + N_{e1}} + K^{all} \sqrt{N_b + N_{e1} + N_{e2}}} \geq \frac{N_{e2}}{N_b + N_{e1} + N_{e2}}. \end{cases}$
	Parameter Selection	$\begin{cases} \beta_1 = \frac{N_b + N_{e1} + N_{e2}}{N_b} \frac{K^b \sqrt{N_b}}{K^b \sqrt{N_b} + K^{b,e1} \sqrt{N_b + N_{e1}} + K^{all} \sqrt{N_b + N_{e1} + N_{e2}}}, \\ \beta_2 N_b + \alpha_1 N_{e1} = \frac{(N_b + N_{e1} + N_{e2}) K^{b,e1} \sqrt{N_b + N_{e1}}}{K^b \sqrt{N_b} + K^{b,e1} \sqrt{N_b + N_{e1}} + K^{all} \sqrt{N_b + N_{e1} + N_{e2}}}, \\ \beta_3 = 1 - \beta_1 - \beta_2, \alpha_2 = 1 - \alpha_1. \end{cases}$
$F^c = F_b \cup F_{e1}$ (Medium resolution)	Fairness Constraints	$\frac{K^b \sqrt{N_b}}{K^b \sqrt{N_b} + (K^{b,e1} + K^{all}) \sqrt{N_b + N_{e1}}} < \frac{N_b}{N_b + N_{e1}}$
	Parameter Selection	$\alpha_1 = \frac{K^{b,e1}}{K^{b,e1} + K^{all}}, \alpha_2 = 1 - \alpha_1.$
$F^c = F_b$ (Lowest resolution)	Fairness Constraints	No constraints on $(K^b, K^{b,e1}, K^{all})$ and $(N_b, N_{e1}, N_{e2})$
	Parameter Selection	$\beta_1 = \frac{K^b}{K^b + K^{b,e1} + K^{all}}, \beta_2 = \frac{K^{b,e1}}{K^b + K^{b,e1} + K^{all}}, \beta_3 = \frac{K^{all}}{K^b + K^{b,e1} + K^{all}}.$

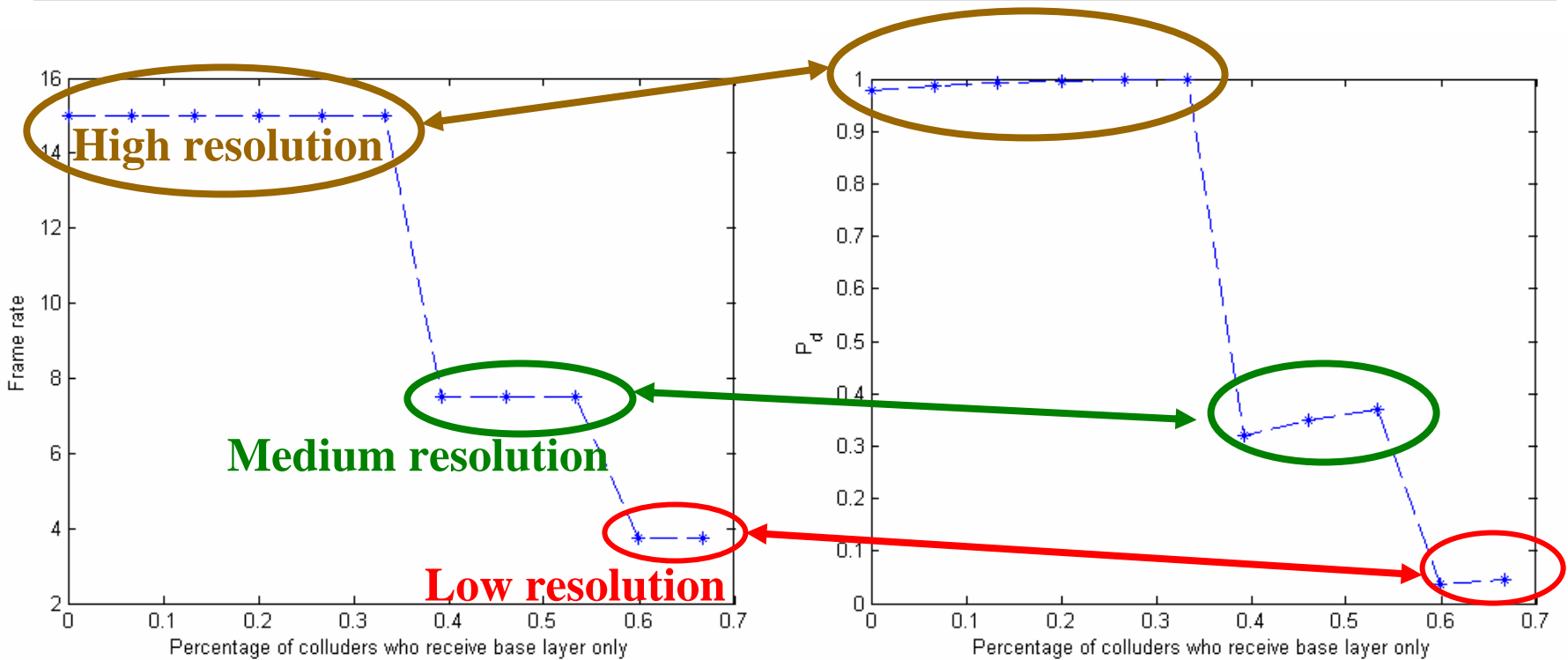
Number of colluders in different subgroups

Length of fingerprints embedded in different layers

A copy of higher resolution → more severe constraints on collusion



# Effectiveness of Collusion



Perceptual quality of the colluded copy

Effectiveness of fair collusion

➤ A colluded copy of higher resolution → larger risk to be detected

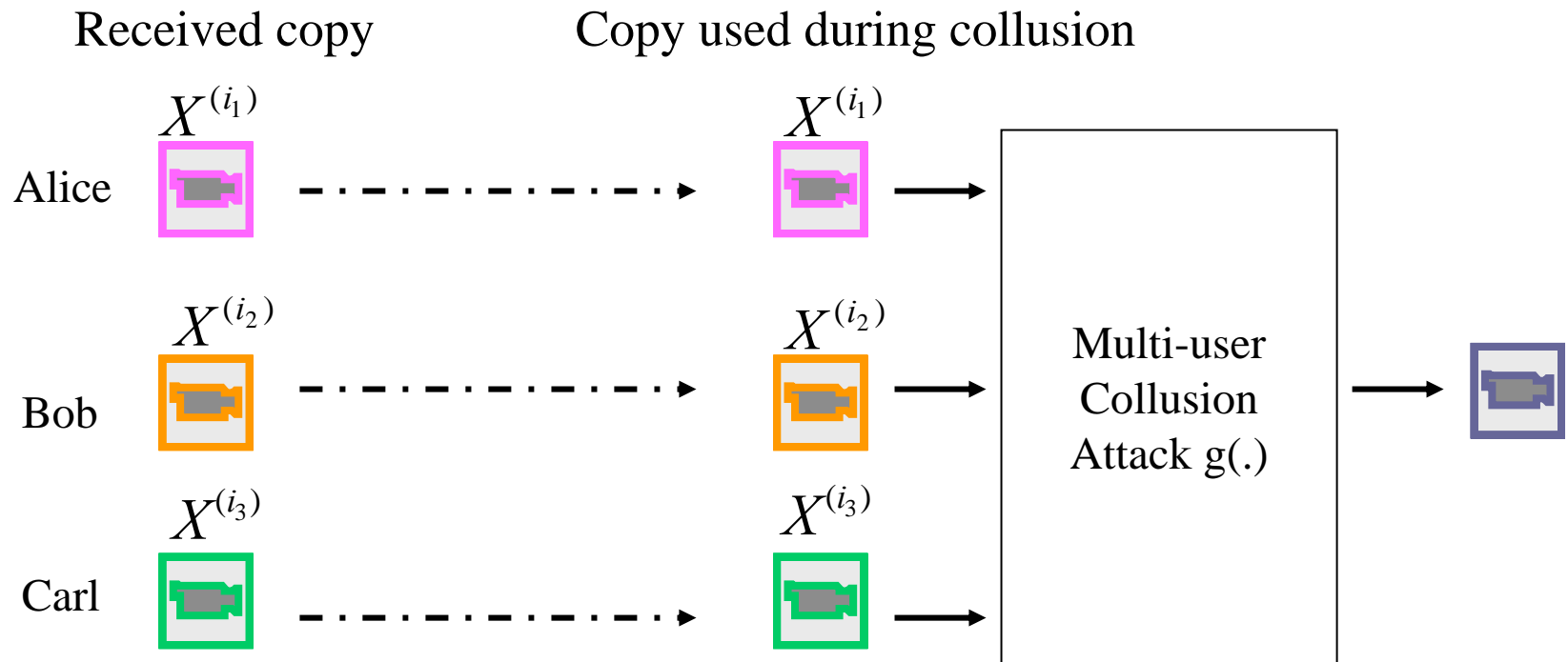


# ***Traitors within Traitors in Multimedia Forensic Systems***



# Assumptions in Prior Work

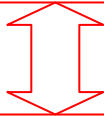
- Assumptions of fair-play during collusion in prior work
  - All colluders keep their agreement of fair collusion
  - Everyone tells the truth of his fingerprinted copy during collusion



# Traitors within Traitors

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- The assumption of fair-play during collusion may not always hold
- Dynamics among attackers during collusion
  - **Selfish colluders** : wish to minimize their own risk of being caught
  - **Other colluders** : wish to protect their own interests
- Formulation and analysis of the dynamics among colluders:
  - Understand the attackers' behavior
  - Build a complete model of multi-user collusion

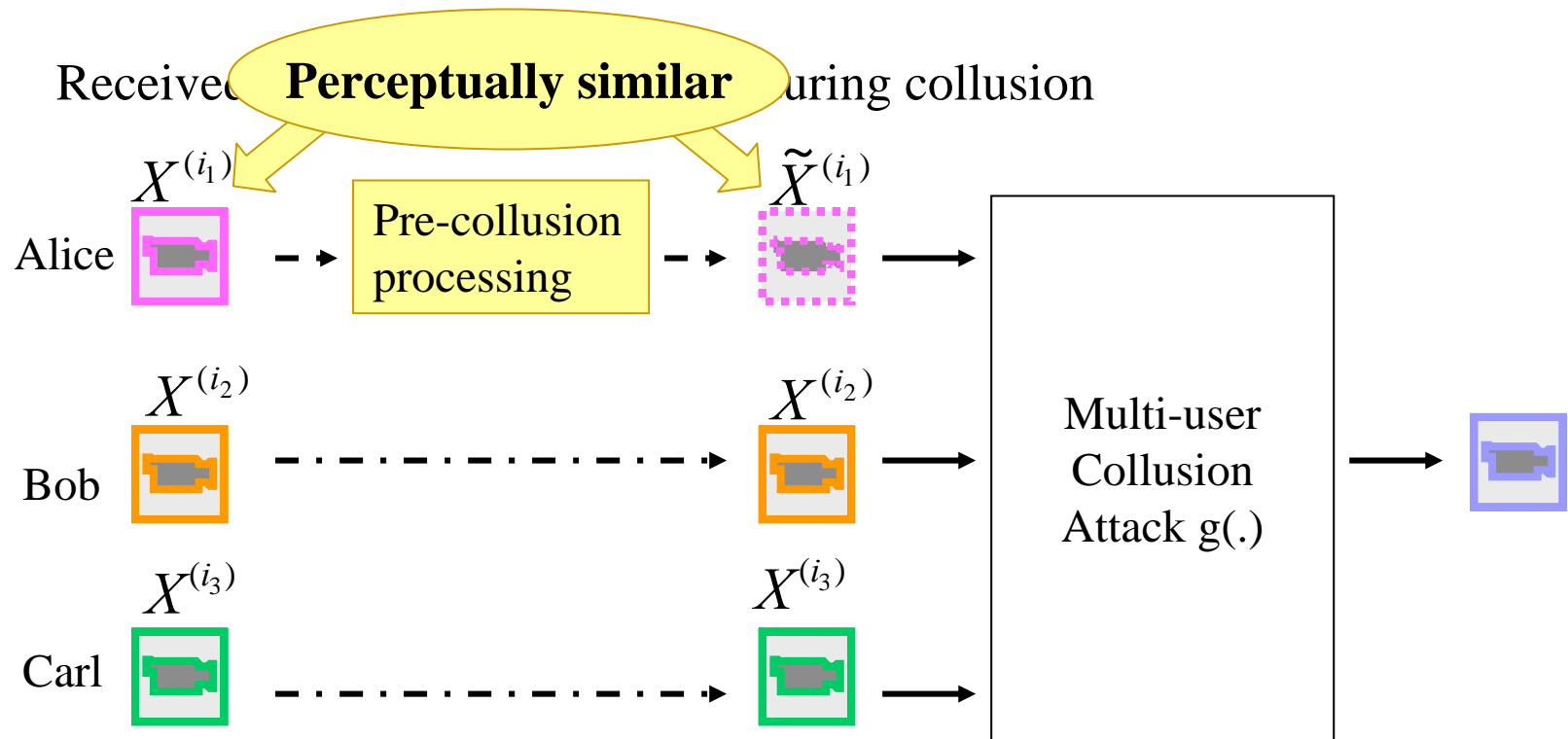




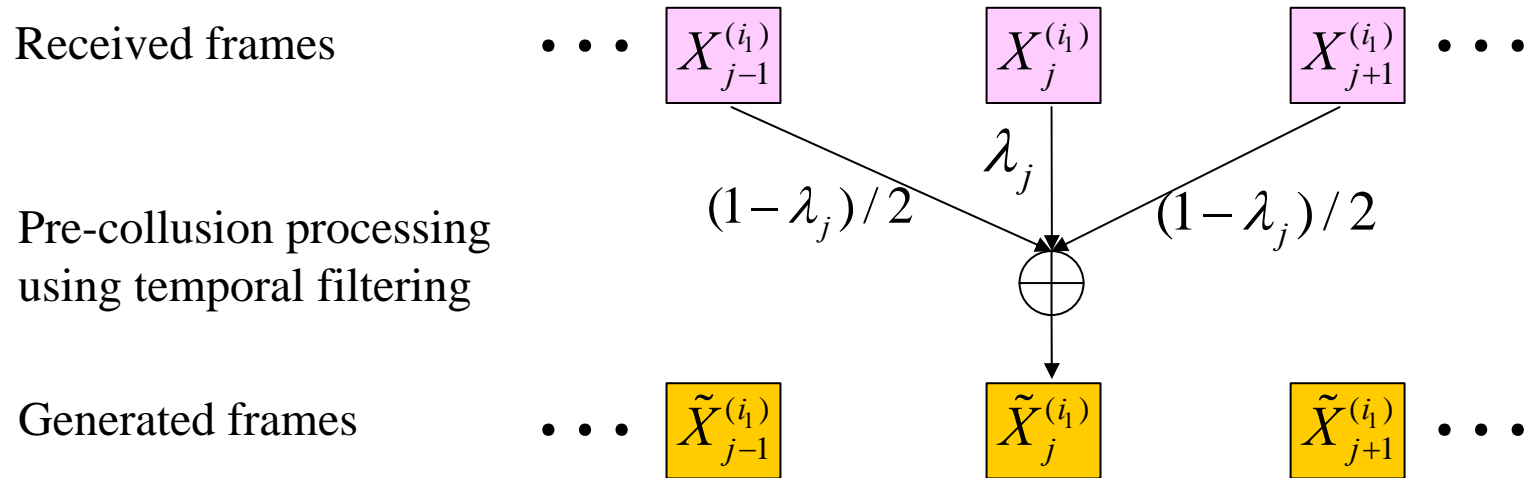
# Risk Minimization by Selfish Colluders

- Selfish colluders:

- Alice processes her fingerprinted copy before multi-user collusion to further reduce her probability of being detected



# Temporal Filtering of Fingerprinted Frames



- **Goal: attenuate the energies of the embedded fingerprints**
  - Replace each segment of the fingerprinted copy with another, seemingly similar segment from different regions of the content
- **Temporal filtering of the received fingerprinted frames**

$$\tilde{X}_j^{(i_1)} = \frac{1-\lambda_j}{2} X_{j-1}^{(i_1)} + \lambda_j X_j^{(i_1)} + \frac{1-\lambda_j}{2} X_{j+1}^{(i_1)}, \quad 0 \leq \lambda_j \leq 1$$



# Performance Analysis

- Perceptual quality of the newly generated frames:

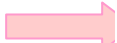
$$MSE_j = \left\| \tilde{X}_j^{(i_1)} - X_j^{(i_1)} \right\|^2 = (1 - \lambda_j)^2 \phi_j / 4$$

- $\phi_j$  is a constant of  $\lambda_j$
  - A larger  $\lambda_j$  is preferred to minimize the perceptual distortion
- 
- The selfish colluder's probability of being detected:
- $$T_N^{(i_1)} = N\left(\mu^{(i_1)}, \sigma_n^2\right), \text{ where } \mu^{(i_1)} = \theta_1 + \sum_j \lambda_j \theta_2(j)$$
- $\theta_1$  and  $\theta_2(j)$  are constants of  $\lambda_j$ ,  $\theta_2(j) \geq 0$
  - A smaller  $\lambda_j$  is preferred to minimize the probability of being detected



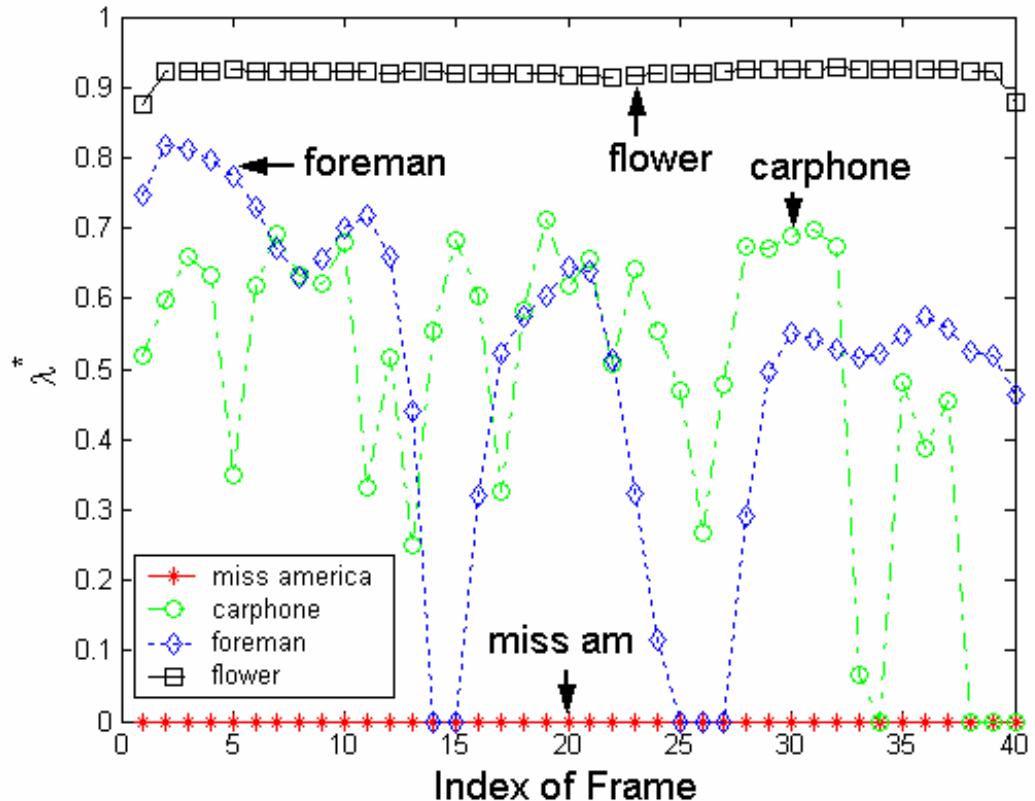
# Selection of the Optimum Filter

- Selfish colluders:
  - tradeoff between the probability of being detected and the perceptual quality of the newly generated copy
- Selection of the optimum filter

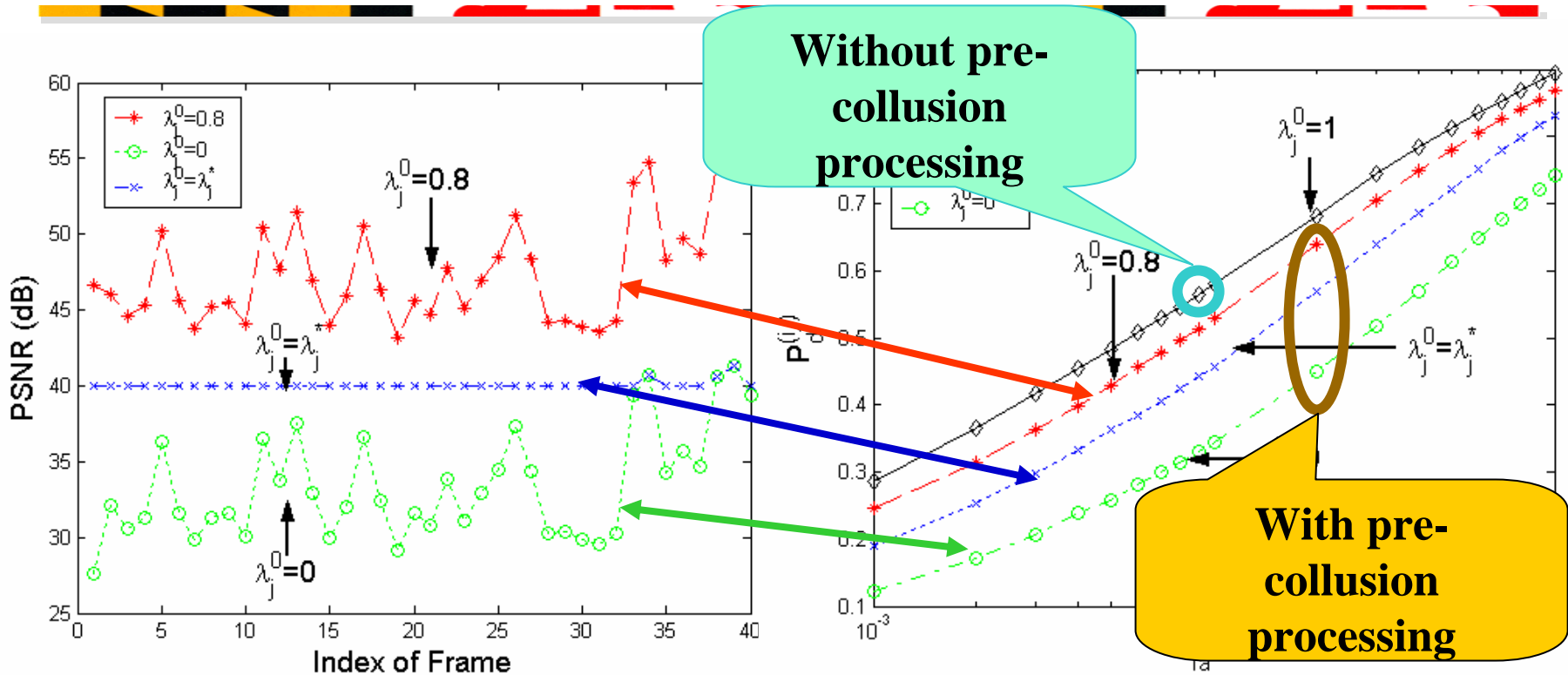
Alice's probability of being detected 

Quality constraints 

$$PSNR_j \geq 40dB$$



# Simulation Results



Perceptual quality of the newly generated copy

The selfish colluder's probability of being detected

- Temporal filtering can further reduce the selfish colluder's risk
- Smaller prob. of being detected → worse perceptual quality



# Summary on Analysis of Dynamics Among Colluders

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- Important to analyze the dynamics among colluders
  - Helps to understand the attackers' behavior during collusion
  - Enables to build a complete model of multi-user collusion
- What we have known:
  - How the colluders achieve the fairness during collusion
  - How a single selfish colluder can further reduce his/her risk
- There are still a lot that we need to learn:
  - How several selfish colluders work together to minimize their risk
  - How other colluders can detect and prevent such selfish behavior during collusion
  - ...
- So we have more work to do...



# Related Publications

- W. Trappe, M. Wu, Z.J. Wang, K.J.R. Liu, “Anti-Collusion Fingerprinting for Multimedia”, *IEEE Trans. on Signal Processing*, special issue on Signal Processing for Data Hiding in Digital Media & Secure Content Delivery, vol. 51, no. 4, pp.1069-1087, April 2003.
- Z.J. Wang, M. Wu, H. Zhao, W. Trappe, and K.J.R. Liu: “Collusion Resistance of Multimedia Fingerprinting Using Orthogonal Modulation”, *IEEE Trans. on Image Proc.*, vol 14, no 6, pp. 804-821, June 2005.
- H. Zhao, M. Wu, Z.J. Wang, and K.J.R. Liu: “Nonlinear Collusion Attacks on Independent Multimedia Fingerprints”, *IEEE Trans. on Image Proc.*, vol 14, no 5, pp.646-661, May 2005.
- Z.J. Wang, M. Wu, W. Trappe, and K.J.R. Liu: “Group-Oriented Fingerprinting for Multimedia Forensics”, *EURASIP Journal on Applied Signal Processing*, special issue on multimedia security and rights management, 2004:14, pp. 2142-2162, Nov 2004.
- M. Wu, W. Trappe, Z.J. Wang, and K.J.R. Liu, ”Collusion-Resistant Fingerprinting for Multimedia”, *IEEE Signal Processing Magazine*, Special Issue on Digital Rights: Management, Protection, Standardization, vol 21, no 2, pp.15-27, March 2004.
- H.V. Zhao and K.J.R. Liu, ”Risk Minimization in Traitors within Traitors in Multimedia Forensics”, Proc. IEEE Int’l Conf. on Image Processing (ICIP), Genoa, Sep. 2005.
- H.V. Zhao and K.J.R. Liu, ”Resistance Analysis of Scalable Video Fingerprinting under Fair Collusion Attacks”, Proc. IEEE Int’l Conf. on Image Processing (ICIP), Genoa, Sep. 2005.





*Thanks you!*

