Abstract—We investigate the transmission properties of a subwavelength plasmonic slot waveguide. We show that the transmission can be accurately calculated using the characteristic impedance of the propagating mode. Using such a model, we show that it is possible to design devices without extensive 3-D Finite-difference time-domain (FDTD) computer simulations. We illustrate the approach with calculations of an asymmetric Fabry–Perot germanium photodetector based on the slot waveguide geometry, showing predicted detector efficiencies as high as 69% despite metallic losses.

Index Terms—Optical planar waveguide components, photodetectors, plasmons.

I. INTRODUCTION

INTEGRATED photonic components that allow propagation of an optical mode at subwavelength size scales are expected to play an important role in bridging the gap between optics and electronics in highly integrated optoelectronic circuits. The properties of propagating modes have recently been investigated for several plasmonic structures, such as the metal nanowire [1]–[3], metal nanoparticle arrays [4]–[6], and metal slot waveguides [7]–[10]. In particular, metal slot plasmonic waveguides were shown to support guided modes with high confinement at infrared wavelengths [7]–[10]. Such structures seem promising for guiding into subwavelength nanoscale photodetectors, as they support a high integration density and propagation lengths in the range of a few microns.

In design of optoelectronic circuits based on this geometry, it is desirable to calculate the transmission and reflection properties when waveguides with different parameters are connected together. The coupling between waveguides of different geometries has recently been studied for 2-D plasmonic waveguides of various geometries [11]–[14] and 3-D metal strips [15], [16]. However, the design of complex 3-D structures typically requires extensive computational efforts with computer-aided tools such as the finite-difference time-domain (FDTD) method.

In this paper, we investigate the transmission and reflection properties of the guided modes in metal slot plasmonic waveguides in propagation through a series of waveguide sections with different core materials. Fig. 1 shows a cross section of a metal slot plasmonic waveguide structure where the region indicated by $\varepsilon_m$ is metal, $\varepsilon_1$ and $\varepsilon_c$ are both dielectrics. This waveguide supports a bound mode where light propagates in the $z$-direction (normal to the plane of the figure). We show that a model that uses the characteristic impedances of different sections together can be used to calculate the transmission and reflection properties of such waveguides, even though the metal properties are quite different from those of similar guides in the microwave regime and significant loss must be included in the analysis. We then show that this model allows the design of complex waveguide structures with desired properties at a minimal computational effort by applying this technique in design of a photodetector based on an asymmetric Fabry–Perot resonator embedded in the waveguide.

II. CHARACTERISTIC IMPEDANCE MODEL

We use a transfer matrix approach that relies on the impedance of the mode to describe the behavior of the fields as they propagate through a series of different waveguides. We note that this model is analogous to the mode-matching approach in microwaves where multiple modes might be considered [17], [18]. However, in the case of the slot waveguide, there exists a range of parameters where the waveguide supports only one bound propagating mode. For such structures, it is possible to use a transfer matrix to relate the coefficients of the forward and backward versions of the propagating mode in a linear fashion, along with the transmission and reflection coefficients at each of the discontinuities along the propagation direction.

Considering only the fundamental mode of each waveguide, we build a network model for the propagation of the fields throughout the whole structure. Applying the boundary conditions of continuity of the tangential electric and magnetic fields...
reduces to

\[(A_i + B_i) = C_{i,i+1}(A_{i+1} + B_{i+1})\]  
\[(A_i - B_i) = C_{i,i+1}\frac{(A_{i+1} - B_{i+1})}{Z_{i+1}}\]

where \(A_i\) and \(B_i\) are the amplitudes of the forward and backward propagating modes, respectively. Elements with subindex \(i\) are located before the junction (i.e., to the left of the junction for waves incident from the left), while those with subindex \((i+1)\) are located after the junction. \(Z_i\) is the characteristic impedance of the waveguide. \(C_{i,i+1}\) is the coupling coefficient that can be calculated by the mode overlap at the junction of the waveguides as

\[C_{i,i+1} = \int_S \hat{e}_{i+1} \times \hat{h}_i \cdot \hat{n} dS\]

where \(\hat{e}_i\) and \(\hat{h}_i\) is the normalized tangential electrical field in the \(i\)th cross section, respectively, \(\hat{n}\) is the propagation direction, \(S\) is the entire cross section of the junction, and it is assumed for our model that

\[\int_S \hat{e}_i \times \hat{h}_{i+1} \cdot \hat{n} dS = \frac{Z_{i+1}}{Z_i}\]

For the structures under investigation, we find from simulations that this approximation is valid to about 5%.

The fields are normalized such that

\[\int_S \hat{e}_i \times \hat{h}_i \cdot \hat{n} dS = 1\]

At the junction between two waveguide cross sections, we obtain a transfer matrix \(T_{i,i+1}\) that relates the forward and backward propagating modes as

\[
\begin{bmatrix}
A_i \\
B_i
\end{bmatrix} = \begin{bmatrix}
1/\tau & \rho/\tau \\
\rho/\tau & 1/\tau
\end{bmatrix} \begin{bmatrix}
A_{i+1} \\
B_{i+1}
\end{bmatrix} = \begin{bmatrix}
T(1,1) & T(1,2) \\
T(2,1) & T(2,2)
\end{bmatrix} = T_{i,i+1}
\]

where

\[\tau = \frac{2Z_{i+1}C_{i,i+1}^{-1}}{Z_i + Z_{i+1}}\]
\[\rho = \frac{Z_{i+1} - Z_i}{Z_i + Z_{i+1}}\]

The impedance of the mode is related to the effective permittivity \(\varepsilon_{\text{eff}}\) and the propagation constant \(\gamma\) by

\[Z_i = \sqrt{\frac{\mu_{\text{eff},i}}{\varepsilon_{\text{eff},i}}} = \frac{j\omega\mu}{\gamma_i}\]

In lossy waveguides, the propagation constant \(\gamma = \alpha + j\beta\) is complex, and so, the characteristic impedance of the waveguide is also complex.

The propagation through a waveguide of length \(L\) can be modeled (for the specific approach, we take later of calculating from the “right” to “left” in the structure) as

\[P_i = \begin{bmatrix}
\exp(\gamma L_i) & 0 \\
0 & \exp(-\gamma L_i)
\end{bmatrix}\]

Several sections of waveguides can be modeled by a transfer matrix analogous to that of a standard transmission line by alternating junction matrices and propagation matrices as

\[
\begin{bmatrix}
A_i \\
B_i
\end{bmatrix} = T_{i,i+1}P_{i+1}T_{i+1,i+2}P_{i+2}\cdots T_{i+n-1,i+n} \begin{bmatrix}
A_{i+n} \\
B_{i+n}
\end{bmatrix}
\]

Thus, by knowing the propagation constants of a given waveguide section, the transmission properties of an arbitrary waveguide can be calculated.

III. NUMERICAL MODELS

We used a 2-D full vectorial mode-solving approach as proposed by Lusse et al. [19] to solve for the properties of the actual propagating modes in each waveguide where the properties of materials are different, hence obtaining the necessary parameters to use in transfer matrix methods. With appropriate initial conditions, these calculations can be executed in a few minutes on a personal computer.

We also used FDTD simulations to verify the values of the propagation constants obtained by the mode-solving approach [20]. The FDTD uses magnetic and electric walls at symmetry planes to reduce the computation effort. Convolution perfectly matched layers (C-PMLs) surround the structure in all directions. For these simulations, the guide is excited by a magnetic dipole located in the core region of the waveguide with a sinusoidal signal wrapped in a Gaussian envelope.

Our study focuses on gold as the metal. We model the gold as a Drude metal and its permittivity is given as

\[\varepsilon(\omega) = 1 - \frac{\omega_p^2}{\omega^2 + i\gamma_p\omega}\]

where \(\omega_p = 1.204 \times 10^{16}\) rad/s and \(\gamma_p = 1.375 \times 10^{14}\) rad/s [21].

The propagation constants from the FDTD were calculated by observing the phase variation and the decay of the mode along the propagation direction. While no attempt was made to mitigate numerical dispersion in the grid, we found a difference in propagation constant of less than 2% between the FDTD and the mode-solving approach. To minimize numerical artifacts in comparing our transfer matrix results to the full FDTD simulations of the structure, we used the propagation constants from the FDTD simulations in calculations involving the impedance model, though we believe, given the agreement between the two approaches, that the faster mode-solving approach is otherwise generally sufficient.

The effective refractive index \(n_{\text{eff}}\) is related to the imaginary part of the propagation constant \(\gamma\) as \(n_{\text{eff}} = \beta c / \omega\). The propagation length \(L_p\) is defined as the length for which the field intensity attenuates by a factor of \((1/e)\) and is related to the real part of the propagation constant \(\gamma\) as \(L_p = 1/2\alpha\). The surrounding material was silicon dioxide for all simulations with a refractive index of 1.44. The dimensions of the waveguide core \((a \times b)\) were 80 nm \(\times\) 80 nm (see inset in Fig. 2). The core of the waveguide was filled with silicon dioxide, silicon,
Fig. 2. Effective refractive index for different filling materials in the core. The inset represents the cross section of the slot waveguide structure. The core region has permittivity \( \varepsilon_c \). (The germanium loss is taken as that at 1.3 \( \mu \)m).

Fig. 3. Propagation length for waveguides with different filling materials in the core. (The germanium loss is taken as that at 1.3 \( \mu \)m).

or germanium. Silicon was taken to have a refractive index of 3.52. Germanium was modeled with a complex refractive index of 4.23 \(+7.8 \times 10^{-2}j\), which corresponds to a power loss absorption coefficient of \( \alpha_G = 7540 \text{ cm}^{-1} \) [22]. (For simplicity of simulation, the germanium loss was taken independently of frequency, though the loss does drop off relatively abruptly for wavelengths longer than \( \sim 1.5 \mu \)m, and there is a slow rise for wavelengths progressively shorter than \( \sim 1.5 \mu \)m. This particular loss number is characteristic of germanium at a wavelength of 1.3 \( \mu \)m.

The propagation constants found with the mode-solving approach for the slot waveguides with different materials filling the core are shown in Figs. 2 and 3. For these dimensions, there exist only one propagating bound mode above cutoff. This mode is quasi-TEM with dominant \( H_y \) and \( E_x \) fields, i.e., the electric field is primarily polarized “horizontally” from one strip to the other and the magnetic field is primarily vertical (see Fig. 1 for coordinate directions).

IV. REFLECTION FROM A FABRY–PEROT STRUCTURE

As a specific structure of interest also for potential applications, e.g., in photodetectors, we consider first a single-slab Fabry–Perot structure embedded in a plasmonic slot waveguide. The structure is shown in Fig. 4. It consists of a slot waveguide where the core region has a different permittivity \( \varepsilon_c \) for a given length \( L \). The dimensions of the waveguide are \((a \times b) = 80 \text{ nm} \times 80 \text{ nm}\). The metal used is gold, and extends to infinity in the positive and negative \( x \)-directions. The ambient material is silicon dioxide, with a refractive index of 1.44. The waveguide core region is filled with silicon of length varying between 100 and 800 \( \text{nm} \). The refractive index of silicon was taken as 3.52, and the silicon is presumed lossless in this simulation. We examined the calculated power reflected from the structure as we varied the cavity length \( L \).

The power reflected at the front surface of the silicon in a full FDTD simulation of this structure was deduced from the standing wave electrical field amplitudes. We use the absolute value of the electric field at position \( z = z_{\text{max}} \), where it has a maximum amplitude, and at position \( z = z_{\text{min}} \), where it has minimum amplitude (assuming propagation in the forward \( z \)-direction and \( z = 0 \) as the front surface of the silicon). We find the reflected power using the ratio of the maximum electric field \( |E|_{\text{max}} \) at position \( z_{\text{max}} \) and the minimum electric field \( |E|_{\text{min}} \) at position \( z_{\text{min}} \). Defining this ratio as

\[
R = \frac{|E|_{\text{max}}}{|E|_{\text{min}}} \tag{11}
\]

the reflected power is given as

\[
|\rho| = \frac{R\exp(-z_{\text{min}}/2L_p) - \exp(-z_{\text{max}}/2L_p)}{R\exp(z_{\text{min}}/2L_p) + \exp(z_{\text{max}}/2L_p)} \tag{12}
\]

where \( L_p \) is the propagation length for a silicon dioxide core waveguide.

We calculated the reflected power expected from the impedance model as

\[
|\rho|^2 = \frac{|T(2,1)|^2}{|T(1,1)|^2} \tag{13}
\]

We compare the results of the FDTD simulations to those from the characteristic impedance model. Fig. 5 presents the
Fig. 5. Reflected power from a Fabry–Perot structure at $\lambda = 1.3 \, \mu \text{m}$ as a function of the length of the silicon core section.

Fig. 6. Reflection spectrum of a Fabry–Perot resonator for a length of 650 nm.

Fig. 7. Reflection spectrum of two coupled Fabry–Perot resonators at $\lambda = 1.3 \, \mu \text{m}$ as a function of their separation distance $L_{\text{gap}}$.

Fig. 8. Asymmetric Fabry–Perot structure. (a) Perspective view. (b) Top view.

reflection as a function of length for a wavelength of 1.3 $\mu \text{m}$. In Fig. 6, we show the reflected spectrum as a function of wavelength in a cavity length $L$ of 650 nm. We note that the reflection as calculated from the characteristic impedance model well describes the behavior of the device. The reflection measured in FDTD simulation was a few decibels lower than what was calculated by the impedance model. This discrepancy can be explained by presuming that power is also coupled into radiation modes and higher order modes below cutoff that are excited at the discontinuities and that were not taken into consideration in our single-mode transfer matrix impedance model.

We calculated the reflection from a structure with two separate pieces of silicon within the guide as a function of their separation distance $L_{\text{gap}}$. In this case, the pieces of silicon are effectively operating as mirrors, forming a Fabry–Perot resonator between them, a resonator that should tune as this separation distance is varied. The two pieces of silicon have the same cross-sectional dimensions (80 nm $\times$ 80 nm) and are each 100 nm long. The reflection at 1.3 $\mu \text{m}$ as a function of the separation length between the two cavities is shown in Fig. 7. The model well describes the reflection of the structure to a few decibels, and again, we expect that the difference between the model and the FDTD simulations may be the result of radiation modes that are neglected in the model.

This transfer matrix model based on the calculated complex mode impedance of the plasmonic metal slot guides, thus offers a useful approach at a greatly reduced computing cost compared to full FDTD simulations of the structure.

V. DESIGN OF STRUCTURES USING THE CHARACTERISTIC IMPEDANCE MODEL

We can apply the impedance model to design a germanium-based photodetector at 1.3 $\mu \text{m}$. The design consists of an asymmetric Fabry–Perot resonator using the first piece of germanium as the front reflector and the primary absorbing region, followed by a back reflector that is designed by alternating different elements of germanium with silicon dioxide spacers, nominally in the form of a Bragg reflector structure (see Fig. 8).

The structure had the same cross section as the one depicted in Fig. 2, with dimensions $a \times b$ of 80 nm $\times$ 80 nm. We used $\text{SiO}_2$ as the surrounding material, with refractive index of 1.44. At 1.3 $\mu \text{m}$, the germanium has a complex refractive
The index of $4.23 + 7.8 \times 10^{-2} j$, which corresponds to a power loss absorption coefficient in bulk germanium of $\alpha_G = 7540 \, \text{cm}^{-1}$ as before.

The back reflector was designed by considering unit cells of the Bragg reflector structure. The unit cell consists of a cross section with silicon dioxide in the core for a propagation length of $L_A$, followed by a similar structure but filled in the core with germanium for a propagation length of $L_B$. The unit cell was designed such that no field would propagate through the entire structure if the unit cell were repeated a large number of times. For the given refractive indexes of silicon dioxide and germanium, a length of 190 nm for both $L_A$ and $L_B$ would create a Bragg back reflector at 1.3 µm.

Using the characteristic impedance model, we then calculated the length of the photodetector $L$ that would maximize the absorbed power in this cross section. For a length of 260 nm, the impedance model shows that the amount of reflected power is less than 1% when two unit cells are used as the Bragg back reflector (as in Fig. 8). The amount of power reflected from the asymmetric Fabry–Perot as a function of the wavelength is shown in Fig. 9. We note that the model correctly predicts the shape of the reflection spectrum and its minimal value at 1.3 µm. The FDTD simulations also showed a reflected power of less than 1% at that wavelength.

The amount of power absorbed in this device by different portions of the structure is shown in Fig. 10, as calculated by the FDTD. There are two loss mechanisms in this structure: the loss due to attenuation of the propagating fields in the metal and the absorption in the germanium semiconductor that contributes to photocurrent. The fraction of power absorbed into a given volume can be calculated from the power flowing into the structure less the power flowing out of it. At 1.3 µm, 30.9% of the power was absorbed in the metal past the front surface. The germanium elements, which represent a volume of $4.1 \times 10^{-3} \, \mu\text{m}^3$ absorbed 69.05% of the total power. The first section of germanium, which consists of a cube of 80 nm × 80 nm × 260 nm absorbed 54.1% of the incoming power. Also, the absorption peak occurs at 1.3 µm, where the photodetector was designed to operate. Assuming full quantum efficiency, this detector would have a responsivity of 0.72 A/W at 1.3 µm.

Such a device could be fabricated from germanium on insulator wafers by first patterning the germanium, and subsequently, depositing metal with a liftoff process. The two metal stripes on each side of the germanium could be used to bias the photodetector and create a metal–semiconductor–metal junction. Light could be coupled at the end of the device by a dielectric waveguide or an optical fiber, or by a nanometallic scatterer located close to the waveguide, though such coupling mechanisms remain subject for further investigation.

VI. CONCLUSION

We presented a simple model to account for the transmission properties of a plasmonic metal slot waveguide with discontinuities in the propagation direction. We showed that this model accurately modeled the properties of interconnected slot waveguides with different materials filling the core region. This model can be readily applied to design structures without extensive time-domain simulations. As an example, we designed an asymmetric Fabry–Perot waveguide photodetector with minimal front surface reflection. The designed photodetector absorbed 69% of the incident power in a volume $4.1 \times 10^{-3} \, \mu\text{m}^3$. We also, therefore, conclude that useful nanoscale photodetectors will be possible by such techniques, and we expect that such devices would have a large electrical operating bandwidth due to their physical size and a corresponding small capacitance.

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